

Cosmological simulations of X-ray heating during the Universe's “Dark Ages”

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Outline

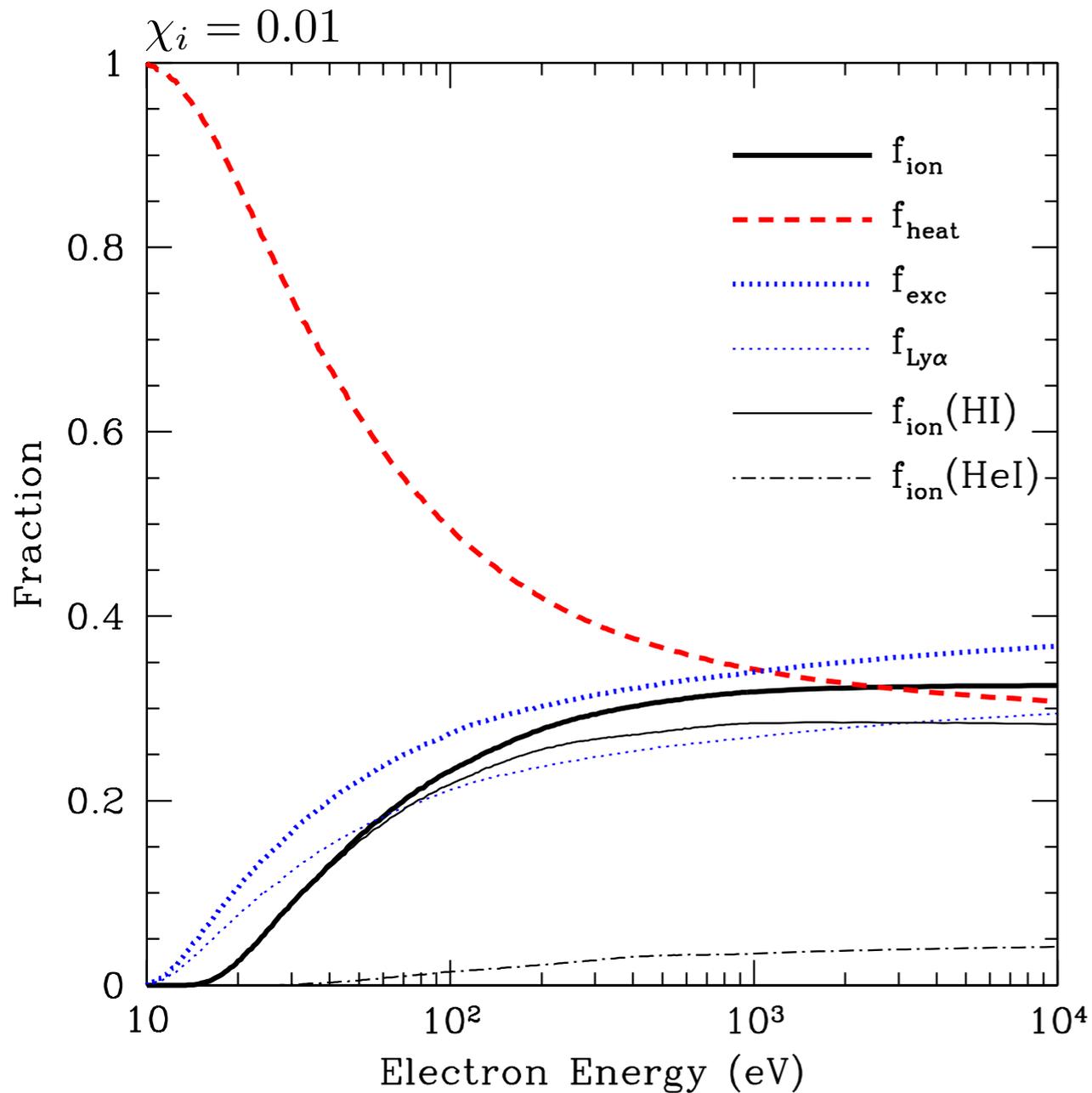
- Introduction: Dark Ages, X-ray heating
- Methods
- Preliminary results
- Future work

Dark Ages/Reionization



Loeb, 2006

X-ray heating



Energy deposition fractions for secondary electrons as a function of energy. From Furlanetto & Stoever, 2010.

- Due to their long mean free paths, X-rays (SN, BH-accretion, PopIII) are expected to be the dominant heating mechanism at high redshift.
- Likely to ionize He, producing fast electrons, $E > 10\text{eV}$.

The 21 cm Signal

- Fundamental quantity - the HI differential brightness temperature:

$$\delta T_b = 27 x_{HI} (1 + \delta) \left(\frac{\Omega_b h^2}{0.023} \right) \left(\frac{0.15}{\Omega_m h^2} \frac{1+z}{10} \right)^{1/2} \left[1 - \frac{T_\gamma(z)}{T_S} \right] \text{ mK}$$

$$\frac{n_1}{n_0} = \frac{g_1}{g_0} e^{-T_\star/T_S}$$

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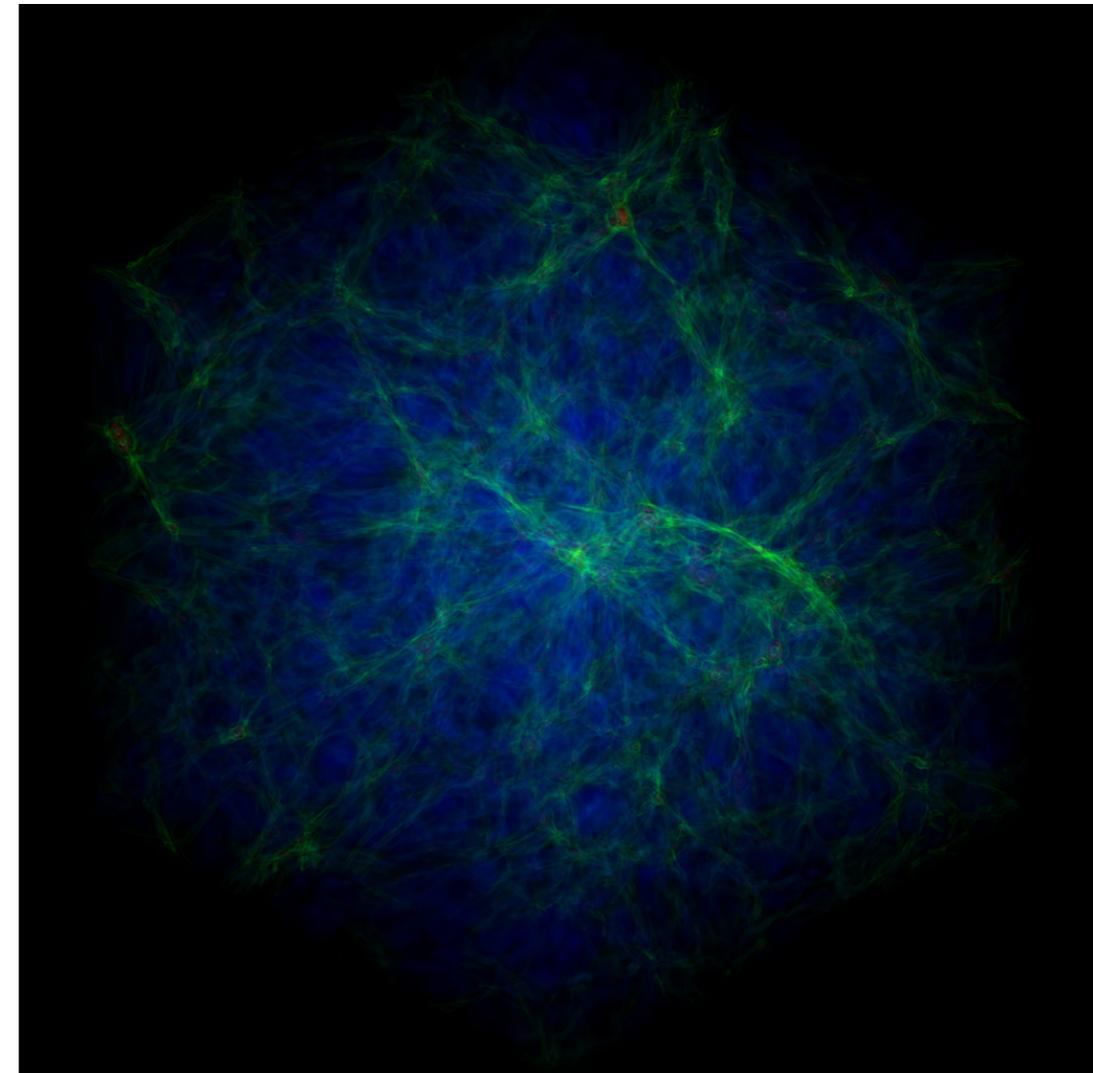
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- Cosmological, hydrodynamics (Eulerian) + N-body, adaptive-mesh-refinement (AMR).
- Adaptive ray-tracing radiative transfer method (Abel & Wandelt 2002)
- Secondary ionizations calculated via Shull & van Steenberg 1985 formulae.



Volume rendering of a cosmological simulation performed with Enzo. Created by Sam Skillman with the AMR analysis toolkit yt, which we also use in this work.

Preliminary Simulations

Cells	Box Size
1024^3	60 Mpc/h



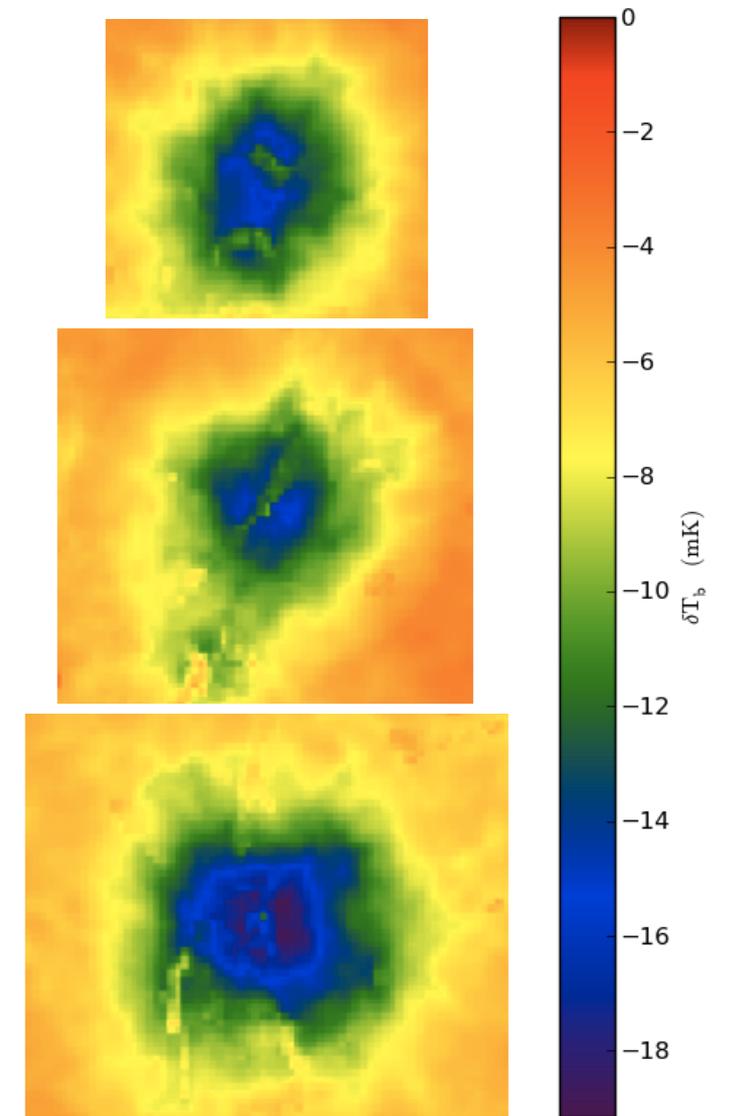
Mass Resolution

$$\sim 1.8 \times 10^7 M_{\odot}$$

- Use friends-of-friends (FOF) halo finder inline with Enzo to populate halos with radiative particles.
- These “MBH” particles are inserted in all halos above threshold mass of $2 \times 10^9 M_{\odot}$ (so they are resolved with > 100 particles).

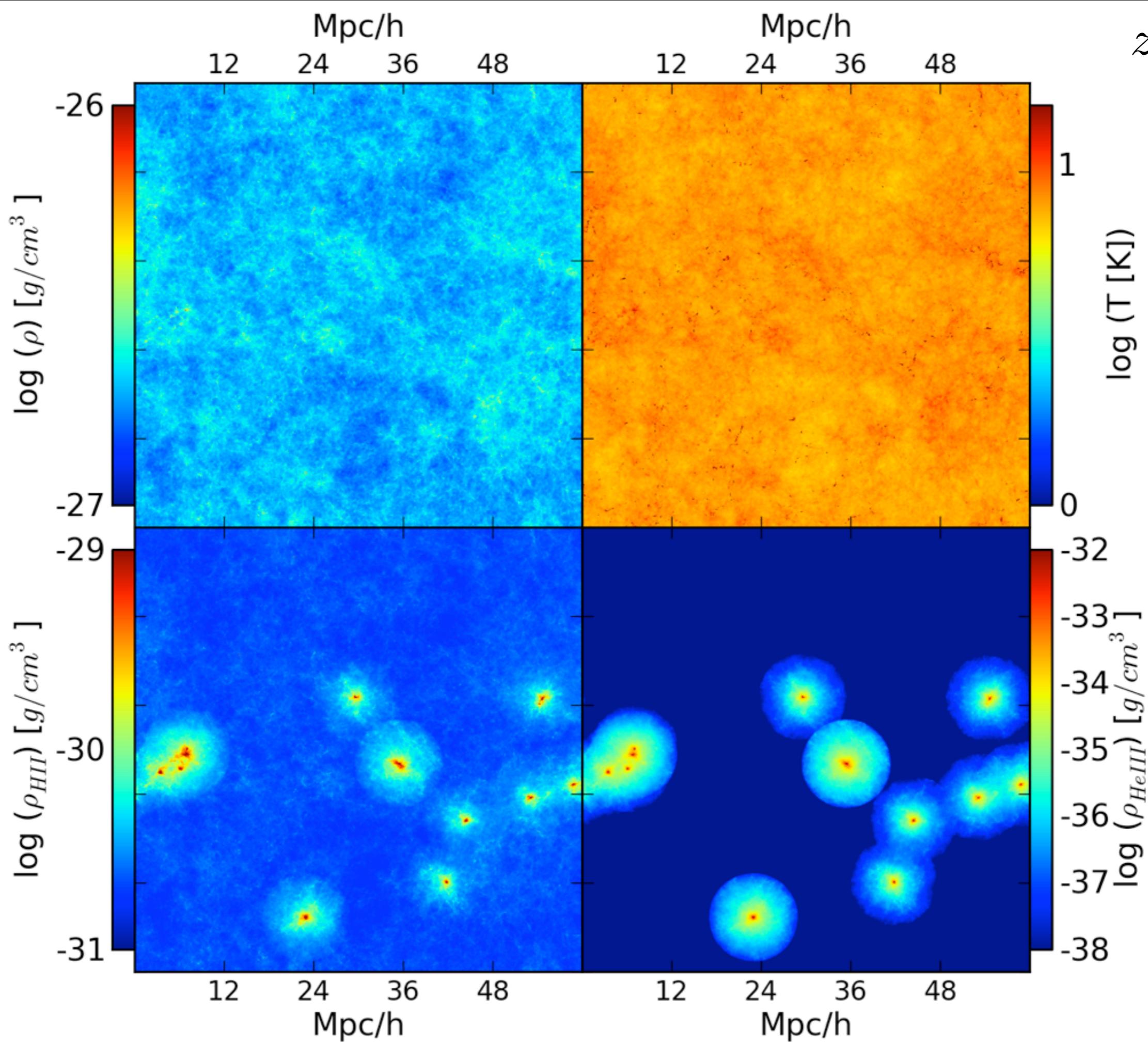
Preliminary Simulations

- Assuming $10^5 M_{\text{sun}}$ black holes undergoing Eddington accretion with a radiative efficiency of 10%.
- Currently using single energy bin spectrum, with 10% of the total luminosity emitted at 0.5 keV.

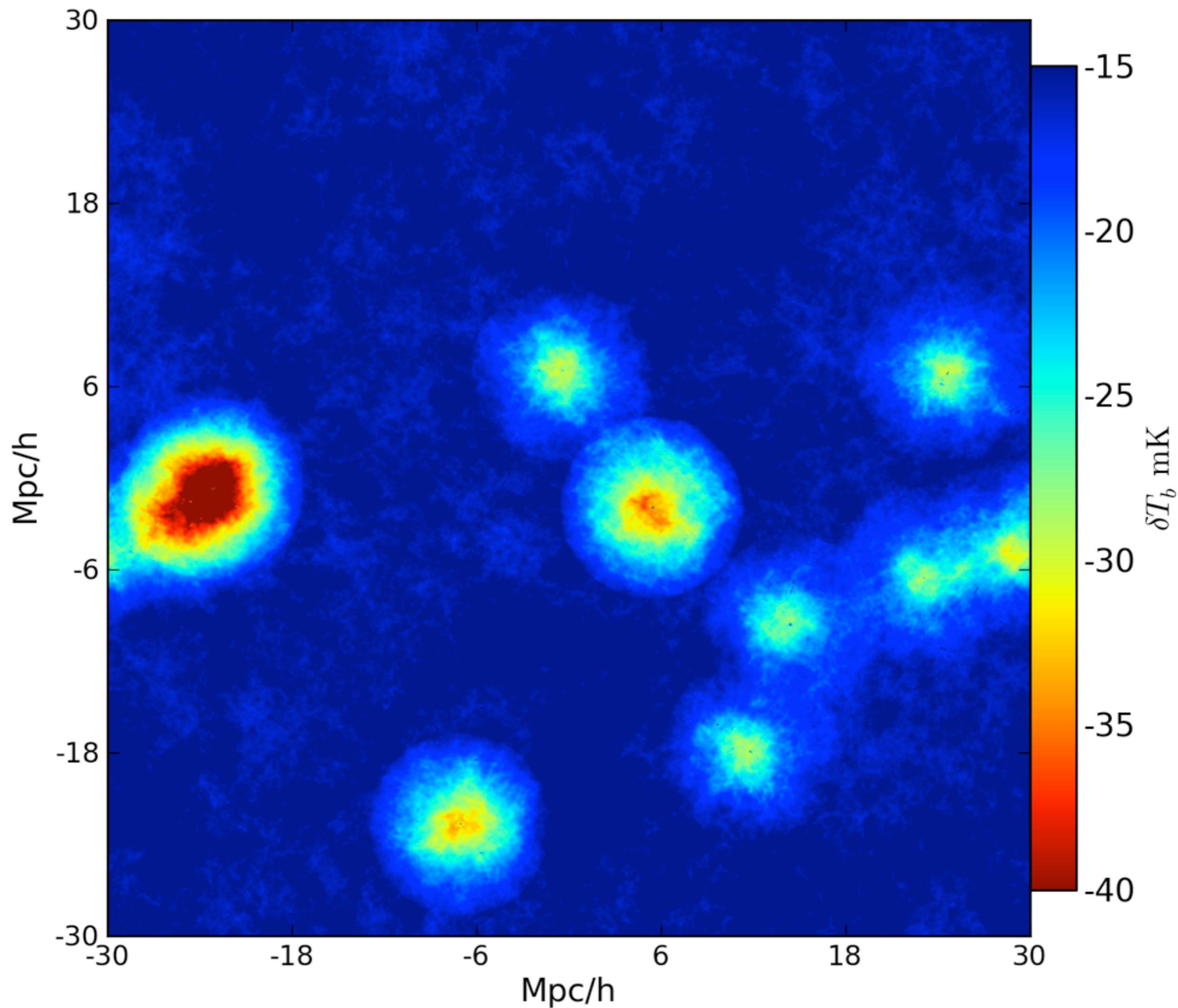


Projections of the differential brightness temperature around individual sources with softer spectra (0.1 - 0.2 keV) from a 256^3 , 20 Mpc/h box test simulation.

$z = 15$

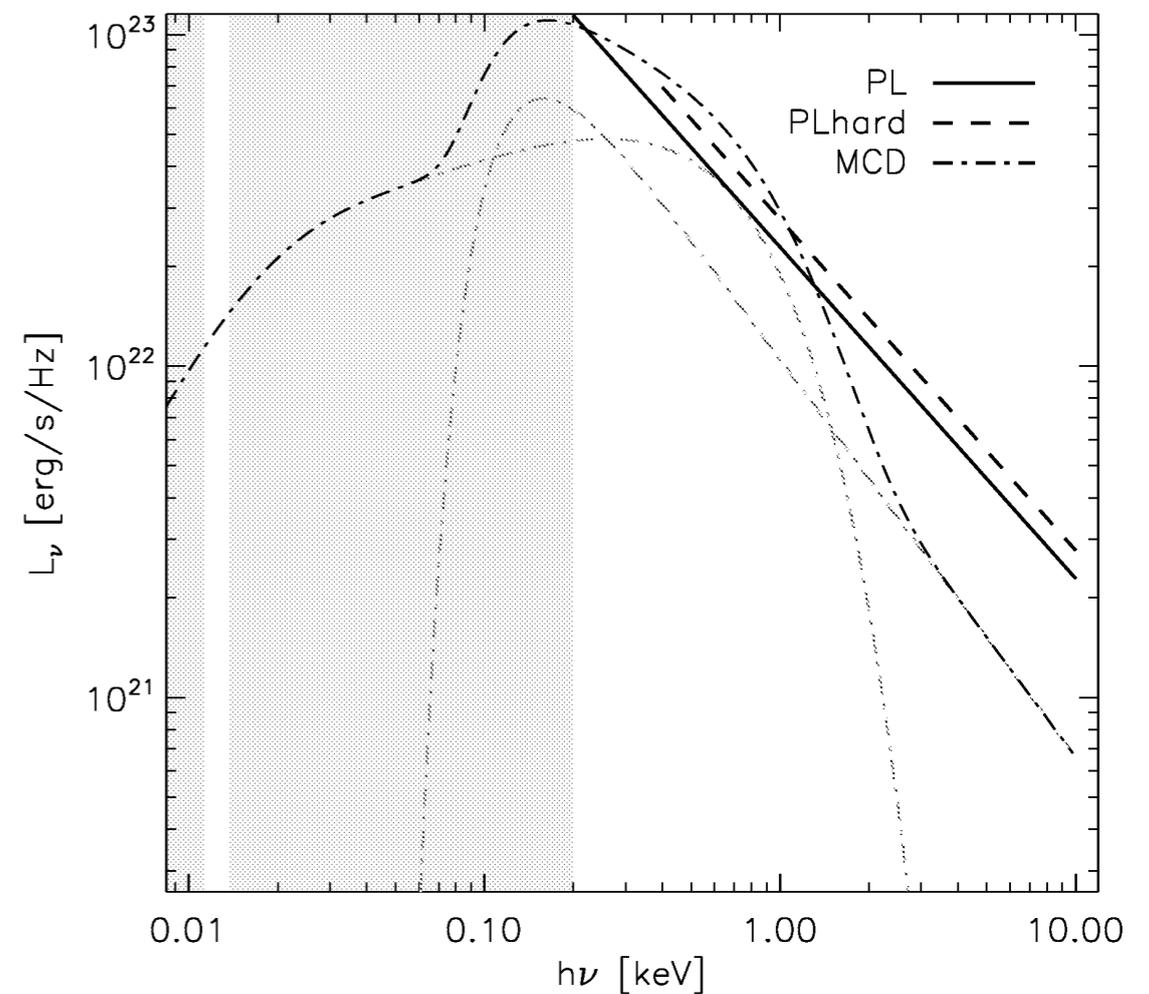


$z = 15$



Upcoming Work

- Future work will implement a more complex, multi-energy bin spectrum.
- Average quasar spectrum of Sazonov et al. 2004 may not be appropriate for high-z. Perhaps adopt ‘miniquasar’ spectrum of Kuhlen & Madau 2005?



Three different spectral templates used to simulate intermediate mass black hole accretion in Kuhlen & Madau, 2005.

Upcoming Work

- Prepare two simulations - one with an abundance of less luminous X -ray sources, another with rare, very luminous sources.
 - Can the global HI signal or angular power spectrum tell them apart reliably?
- Larger volume to improve statistical sampling of the halo mass function more grid cells to maintain (or enhance) mass resolution.

Acknowledgements

- Special thanks to John Wise and Tom Abel for guidance using the adaptive ray tracing scheme in Enzo.
- Additional thanks to Britton Smith and Stephen Skory for their insights on simulating the universe at high redshift.

References

Abel, T. & Wandelt, B. D. 2002, MNRAS, 330, L53

Furlanetto, S. R. & Stoever, S. J. 2010, MNRAS, 404, 1869

Kuhlen, M. & Madau, P. 2005, MNRAS, 363, 1069

Shull, J. M. & van Steenberg, M. E. 1985, ApJ, 298, 268

Wise, J. H. & Abel, T. 2008, ApJ, 685, 40

Radiative Transfer

- Method: Adaptive Ray Tracing (Abel & Wandelt 2002, Wise & Abel 2008)
- Conserve photon flux along rays, branching only when necessary to maintain accuracy of integration.

$$\frac{1}{c} \frac{\partial N_p}{\partial t} + \frac{\partial N_p}{\partial r} = -\kappa N_p$$

R.T.E. for the photon number flux, N_p , and absorption coefficient, κ .

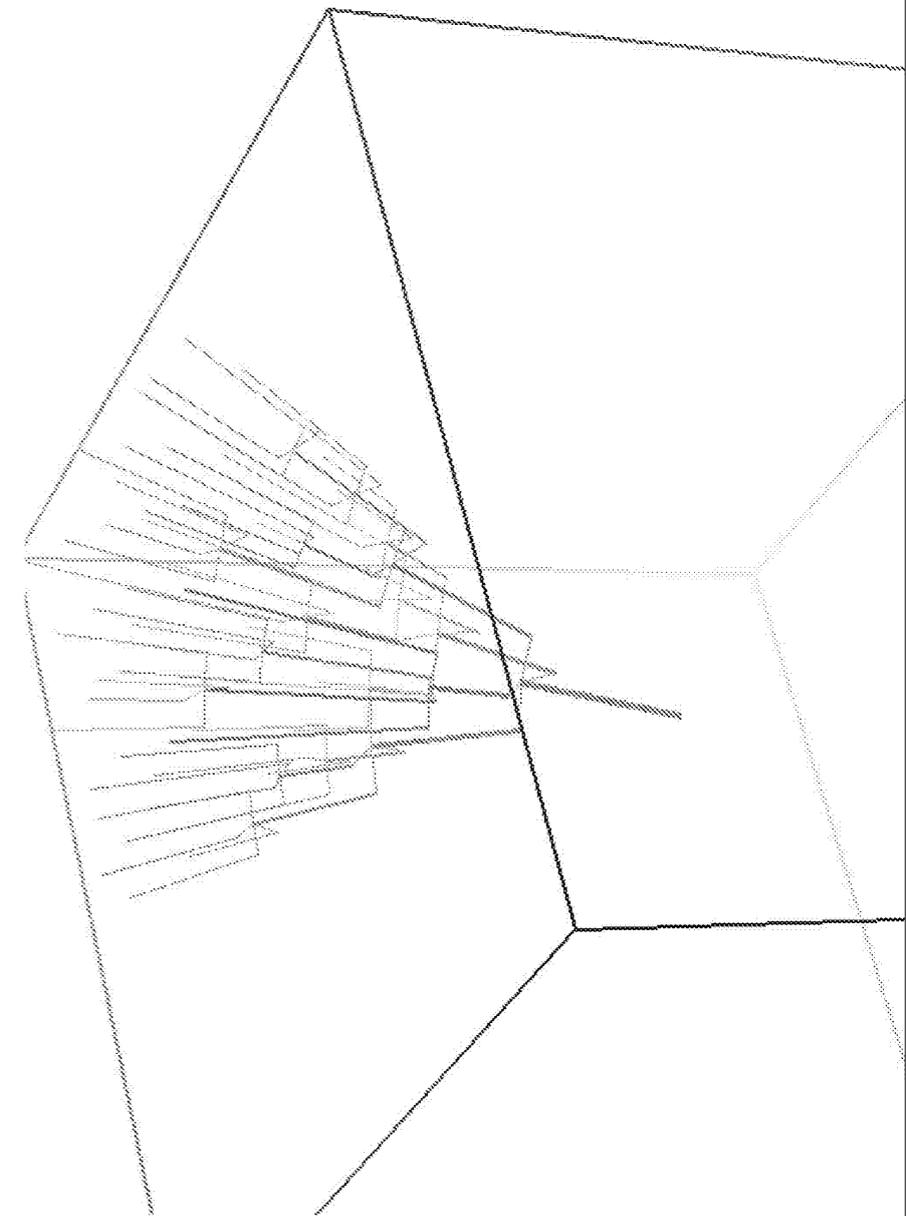
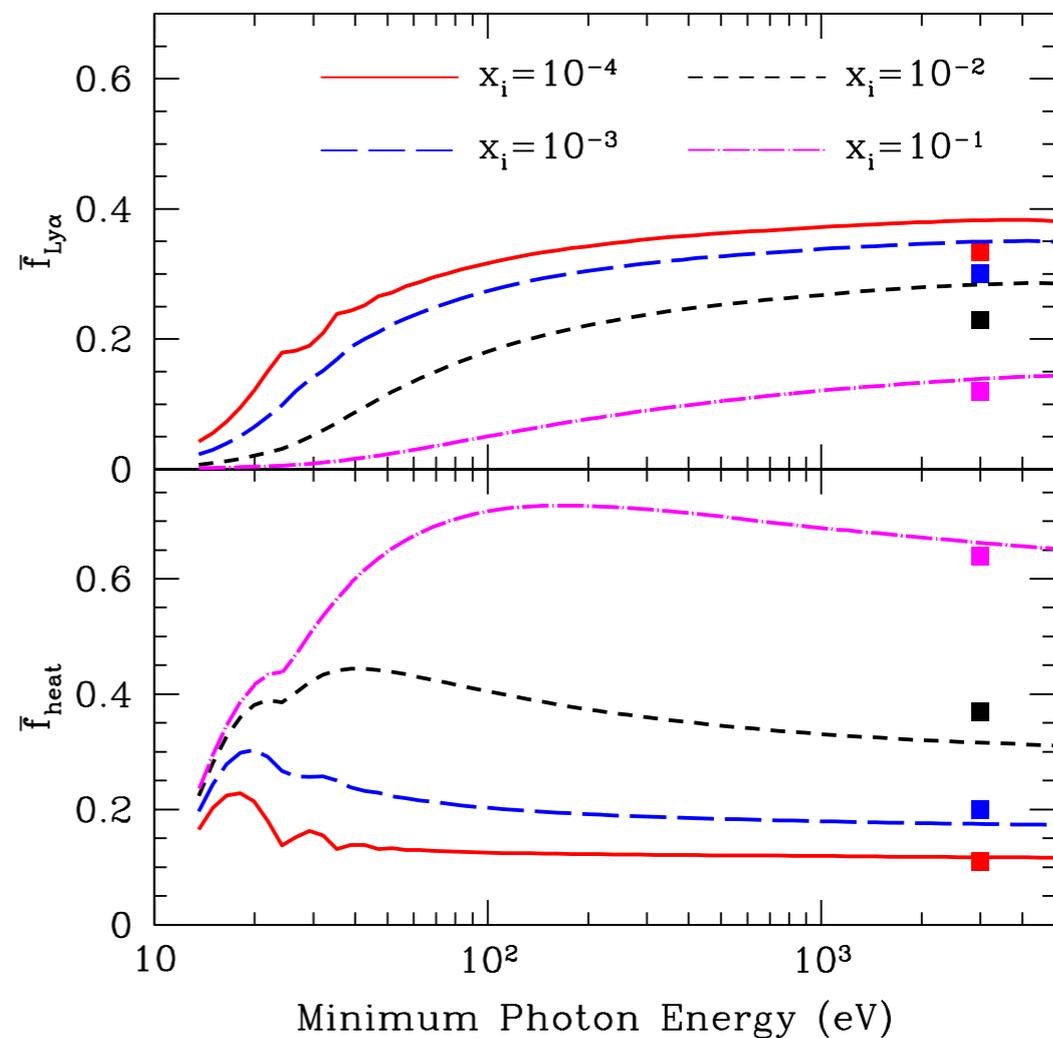
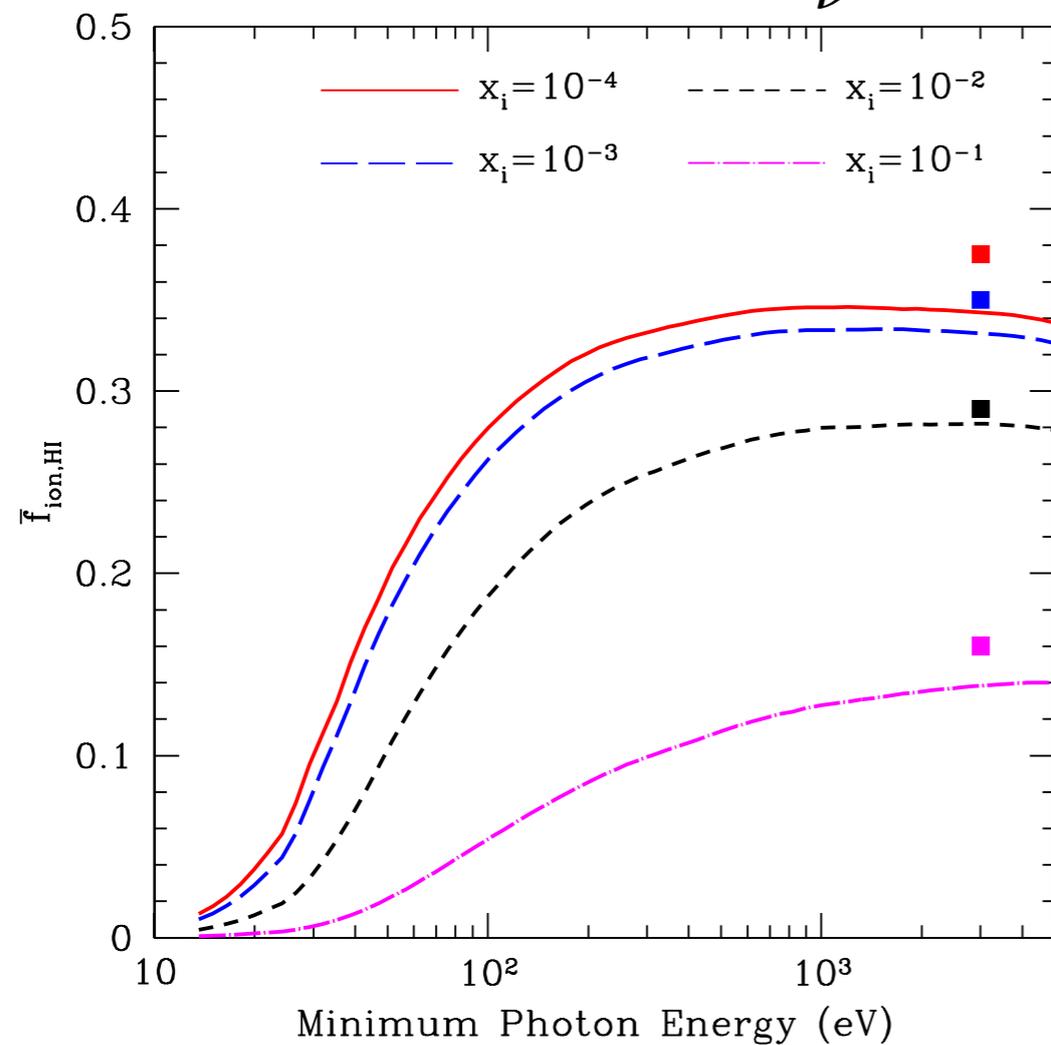


Illustration of a single parent ray spawning many child rays to sample the underlying grid. From Abel & Wandelt, 2002.

X-ray heating

$$L_\nu \propto \nu^{-\alpha}; \alpha = 1.5$$



Energy deposition fractions in ionization, Lyman-alpha, and heat for secondary electrons integrated over sample power law UV/X-ray spectrum. From Furlanetto & Stoever, 2010.

Calculating T_s

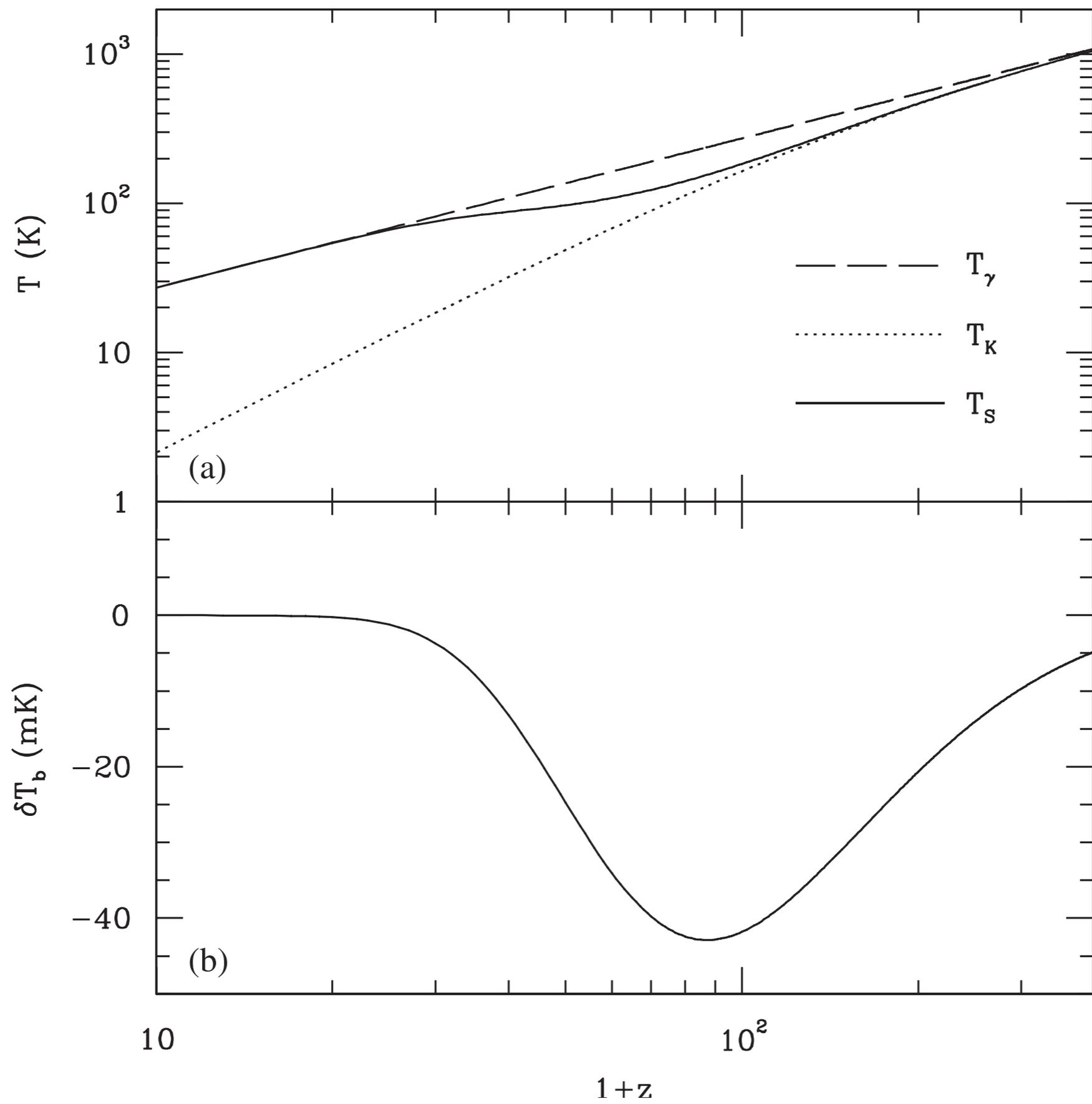
- Enzo is able to track e^- , HI, HII, HeI, HeII, and HeIII abundances in each grid cell.
- Vital in calculating T_s , since H- e^- and H-H collisions are the dominant means of mixing hyperfine levels.

$$T_s^{-1} \approx \frac{T_\gamma^{-1} + x_c T_K^{-1}}{1 + x_c}$$

T_s also depends on x_α , a coupling coefficient for UV scattering, and T_c , the UV color temperature. We neglect them now since sources emit at 0.5 keV only.

$$x_c^i = \frac{n_i \kappa_{10}^i T_\star}{A_{10} T_\gamma}$$

Coupling coefficient for species i , x_c^i , where κ_{10}^i is the rate coefficient for spin de-excitation for species i (Furlanetto, 2006).



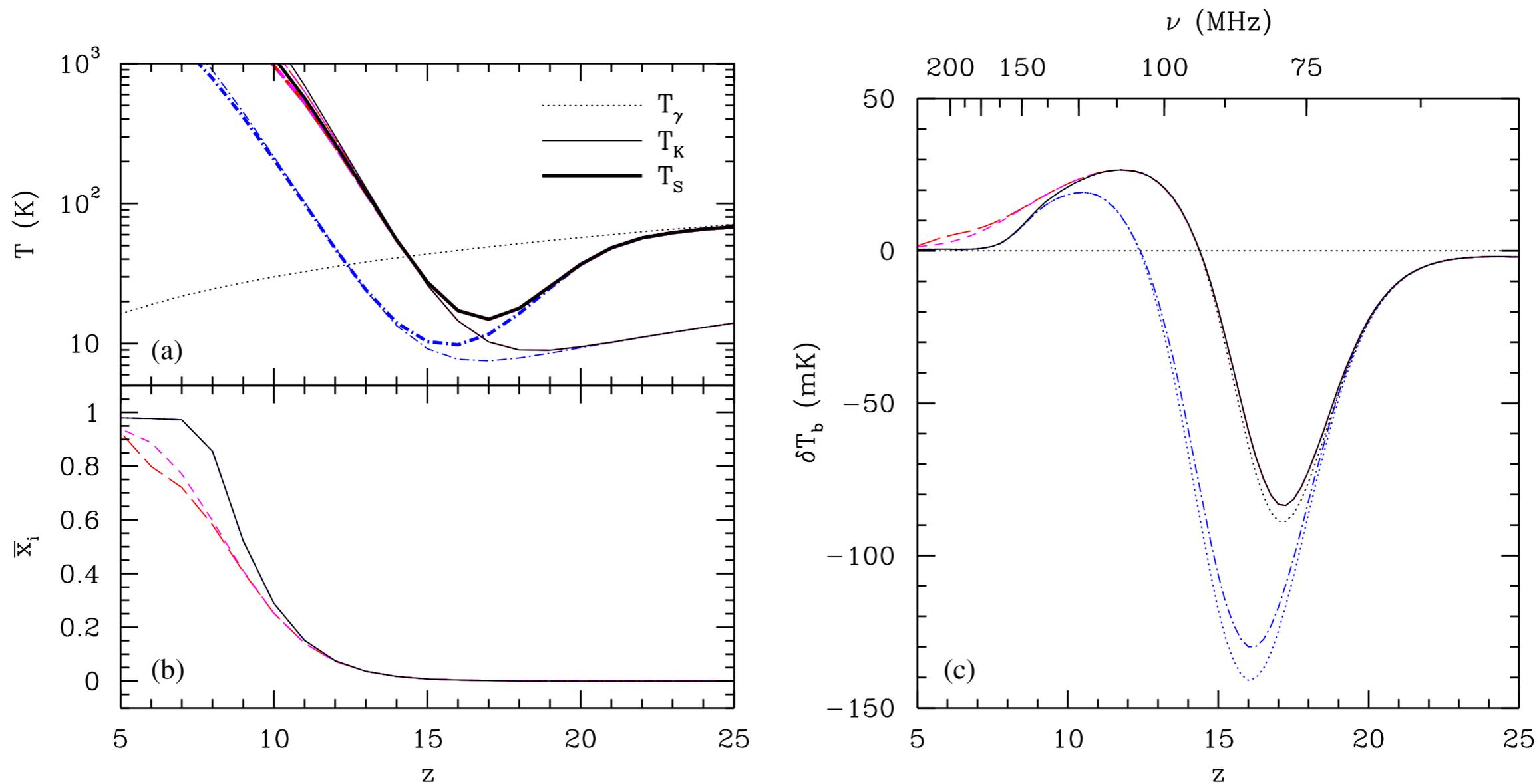


Fig. 7. Global IGM histories for Pop II stars. The solid curves take our fiducial parameters without feedback. The dot–dashed curve takes $f_X = 0.2$. The short- and long-dashed curves include strong photoheating feedback: (a) thermal properties; (b) ionized fraction; (c) differential brightness temperature against the CMB. In this panel, the two dotted lines show δT_b without including shock heating. From [270].