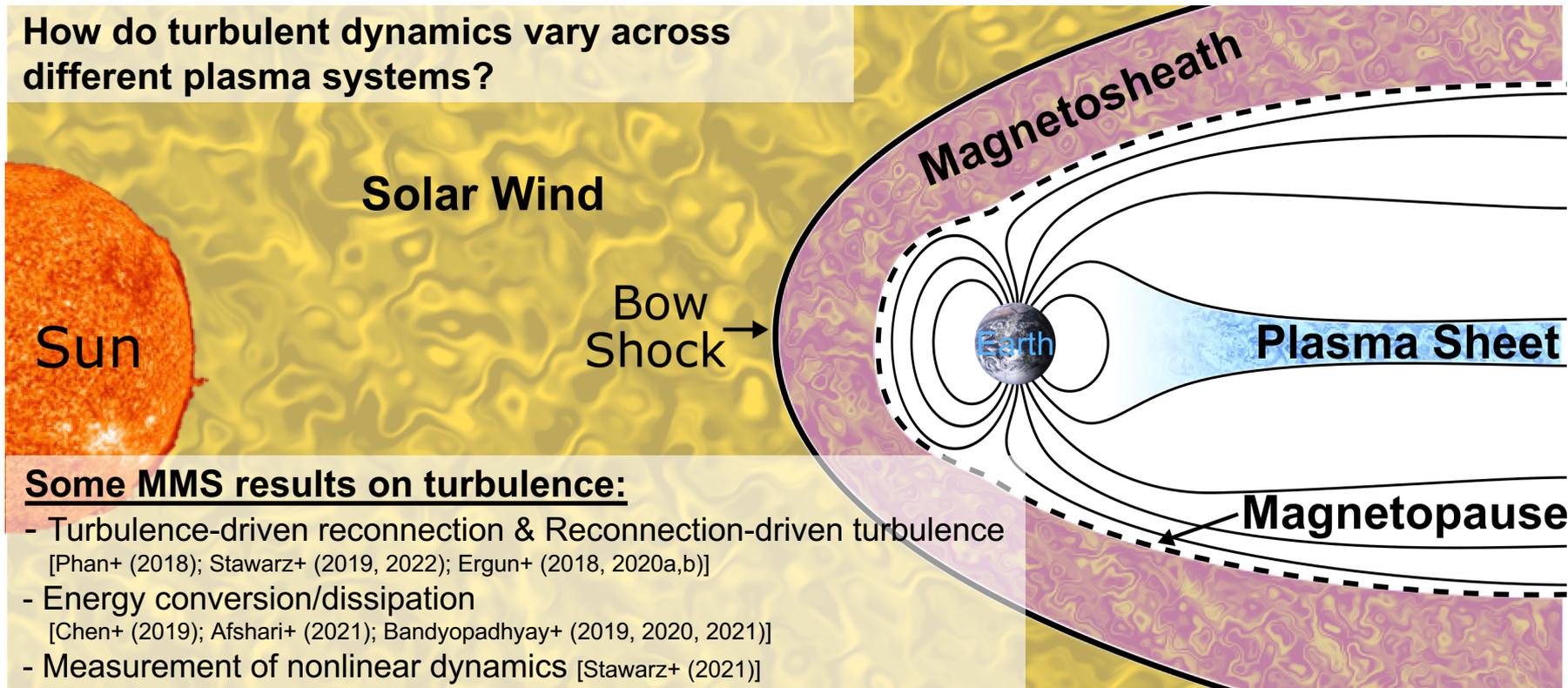




# Magnetosheath Turbulence: Similarities & Differences with Turbulence in the Solar Wind

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How do turbulent dynamics vary across different plasma systems?



## Some MMS results on turbulence:

- Turbulence-driven reconnection & Reconnection-driven turbulence [Phan+ (2018); Stawarz+ (2019, 2022); Ergun+ (2018, 2020a,b)]
- Energy conversion/dissipation [Chen+ (2019); Afshari+ (2021); Bandyopadhyay+ (2019, 2020, 2021)]
- Measurement of nonlinear dynamics [Stawarz+ (2021)]

## Taylor Hypothesis in the Magnetosheath

## Correlation Lengths

## Bulk Alignment Properties

Cross Helicity & Residual Energy

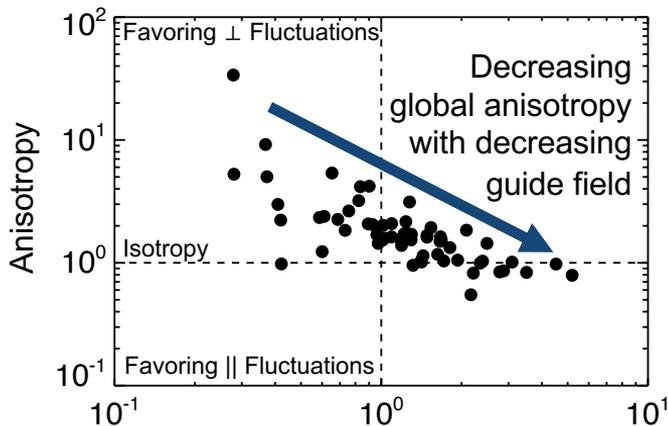
## Intermittency & Small-Scale Structures

# Taylor Hypothesis in the Magnetosheath

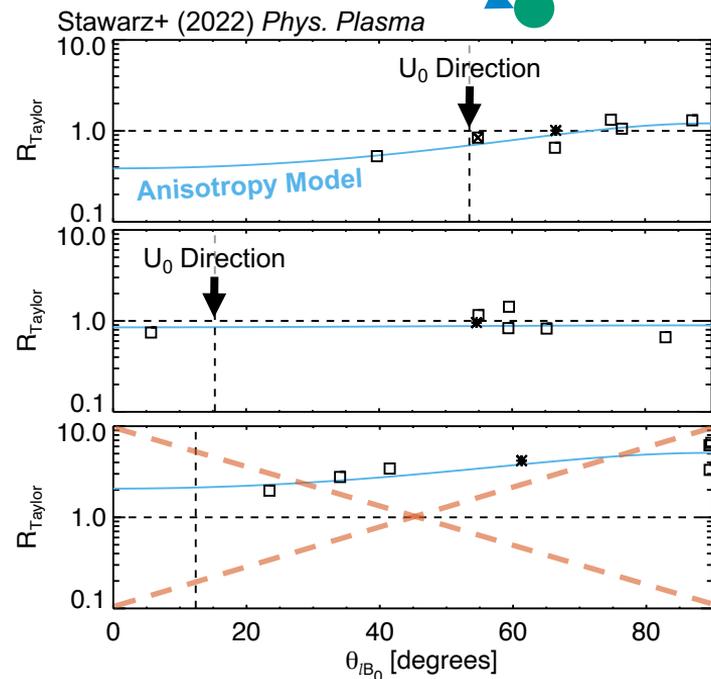
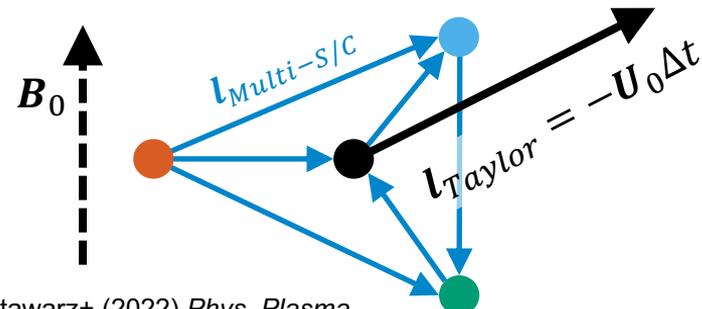
Taylor hypothesis tested by comparing single and multi-spacecraft 2<sup>nd</sup>-order structure functions

$$S_2(\mathbf{l}) = \langle |\mathbf{B}(\mathbf{x} + \mathbf{l}) - \mathbf{B}(\mathbf{x})|^2 \rangle$$

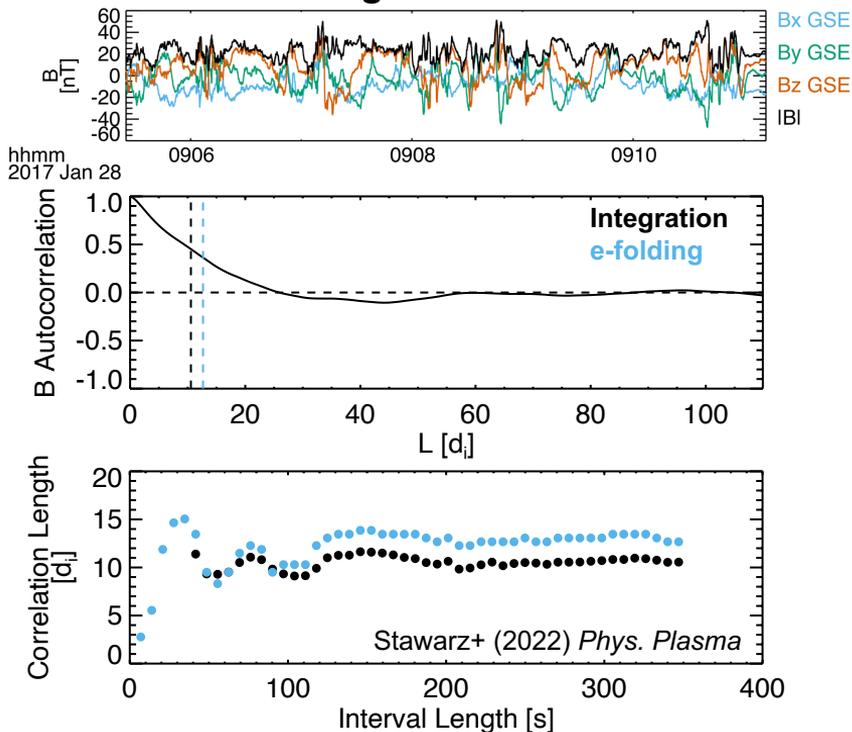
$$R_{Taylor}(\theta) = S_2(\mathbf{l}_{Taylor}) / S_2(\mathbf{l}_{Multi-s/c})$$



Stawarz+ (2022) *Phys. Plasma*  $\delta b_{rms}/B_0$



## Magnetosheath

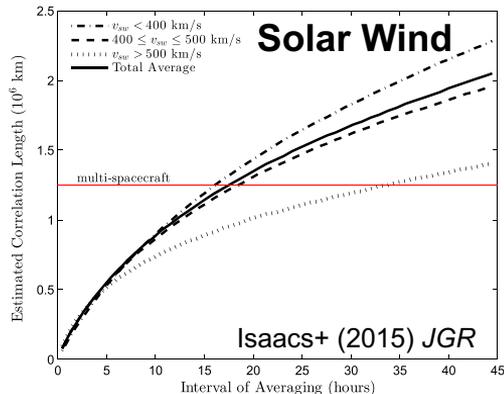


Correlation length defined as:

$$\lambda_c(\theta) = \int_0^\infty A(l) dl$$

$$\text{with } A(l) = \frac{\langle \delta \mathbf{b}(x+l) \cdot \delta \mathbf{b}(x) \rangle}{\langle |\delta \mathbf{b}(x)|^2 \rangle}$$

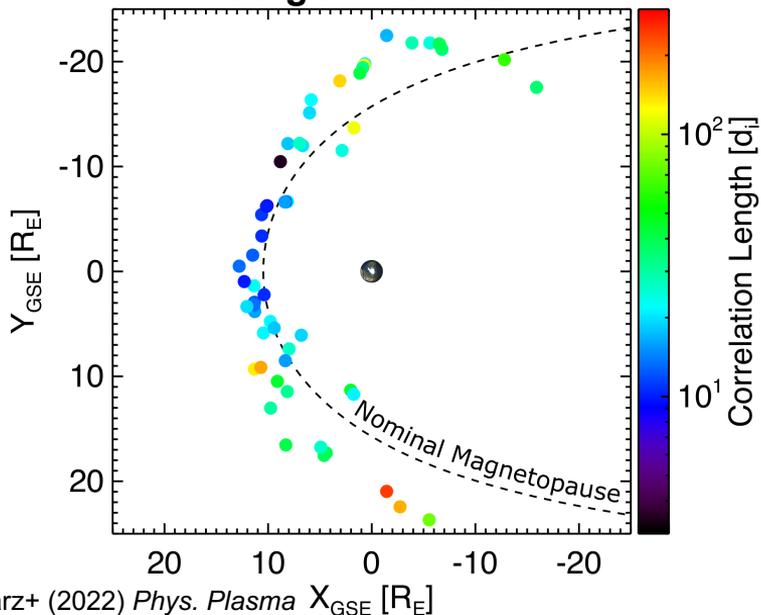
Characteristic size of largest turbulent structures  
– set by driving scale or inverse cascade



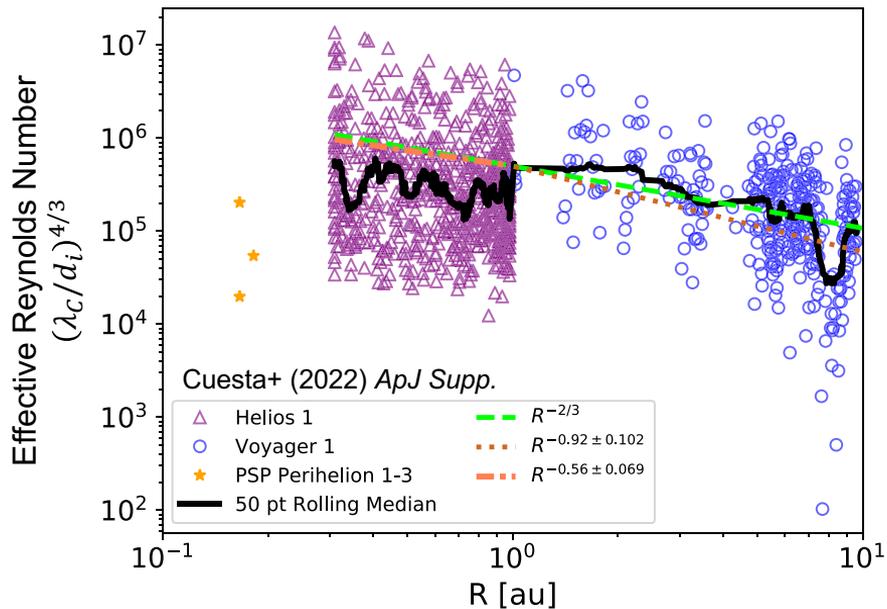
While  $\lambda_c$  converges to a value in magnetosheath, it continues to grow with interval length in solar wind

# Turbulence Correlation Length

Magnetosheath



Solar Wind

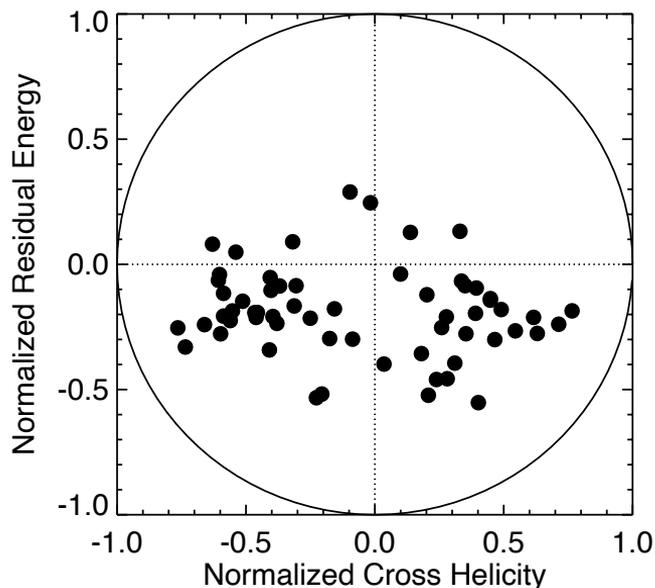


# Cross Helicity & Residual Energy

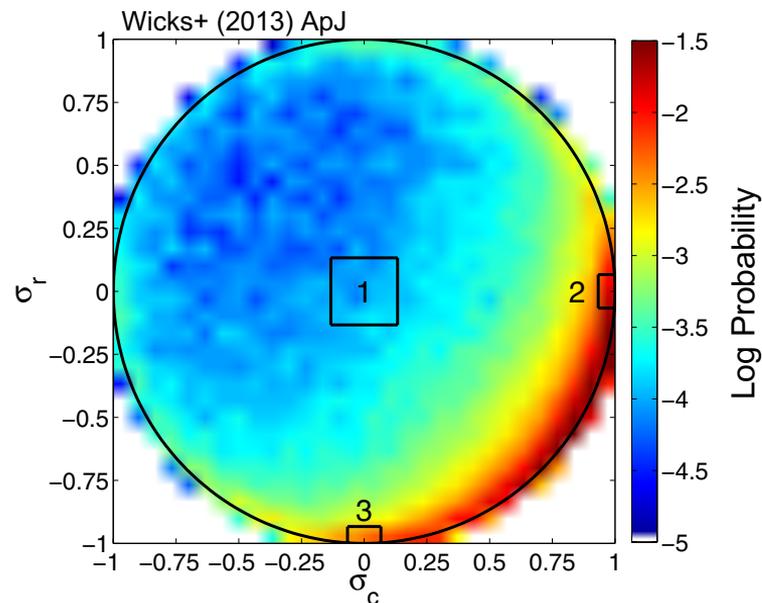
$$\sigma_C = \frac{2\langle \delta \mathbf{u} \cdot \delta \mathbf{b} \rangle}{\langle |\delta \mathbf{u}|^2 + |\delta \mathbf{b}|^2 \rangle}$$

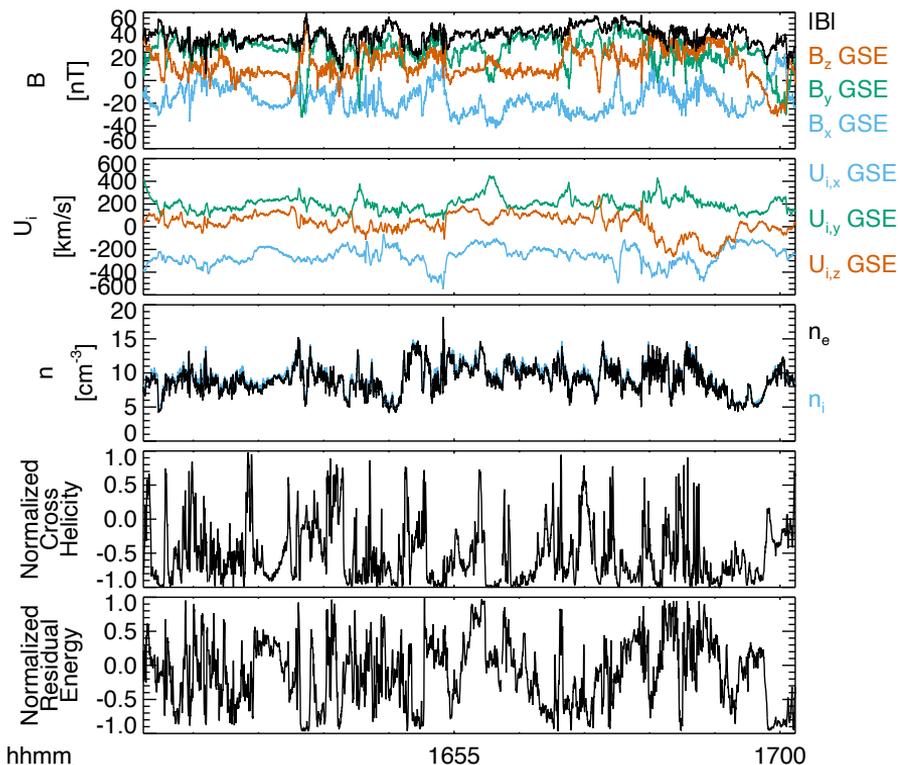
$$\sigma_R = \frac{\langle |\delta \mathbf{u}|^2 - |\delta \mathbf{b}|^2 \rangle}{\langle |\delta \mathbf{u}|^2 + |\delta \mathbf{b}|^2 \rangle}$$

**Magnetosheath**

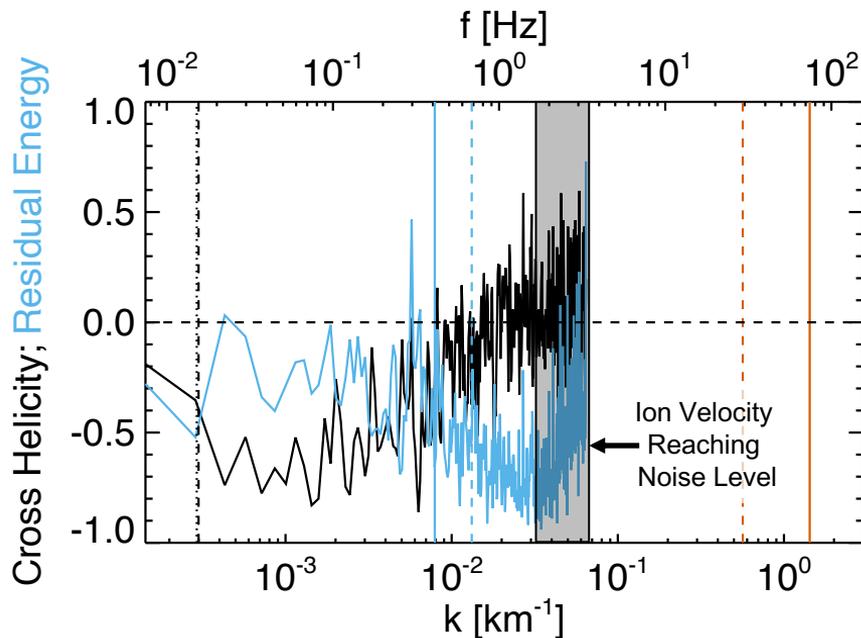


**Solar Wind**

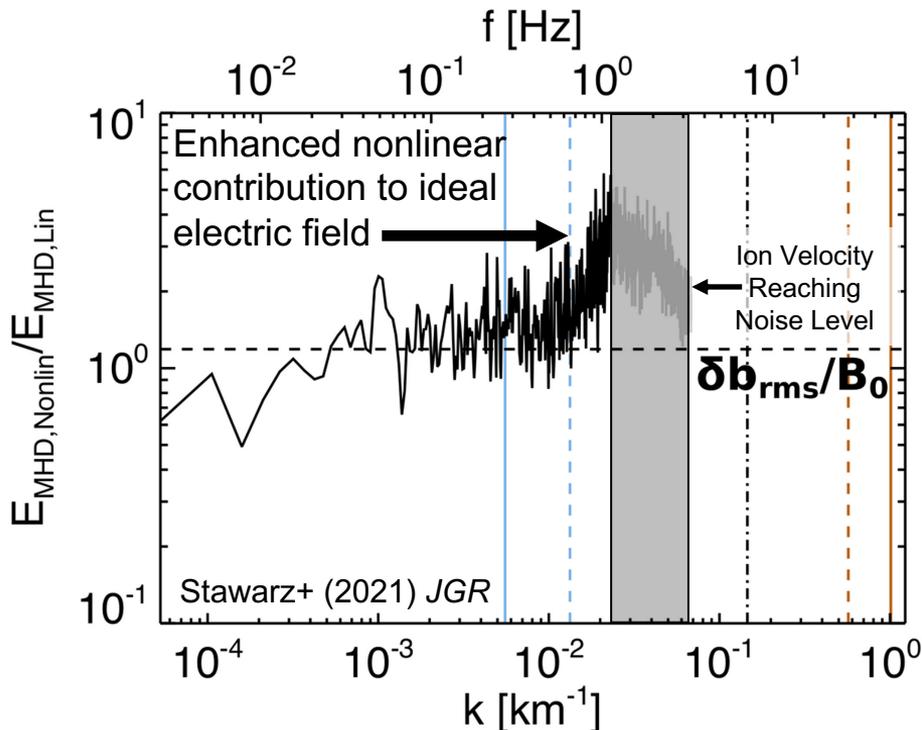
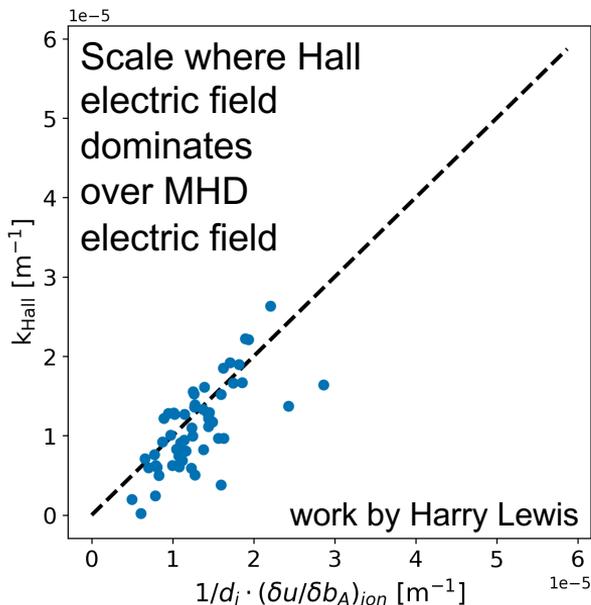




$\sigma_C$  and  $\sigma_R$  are 'patchy' in space and vary as a function of scale



$\sigma_C$  and  $\sigma_R$  can impact the nonlinear turbulent dynamics



# Solar Wind Intermittency

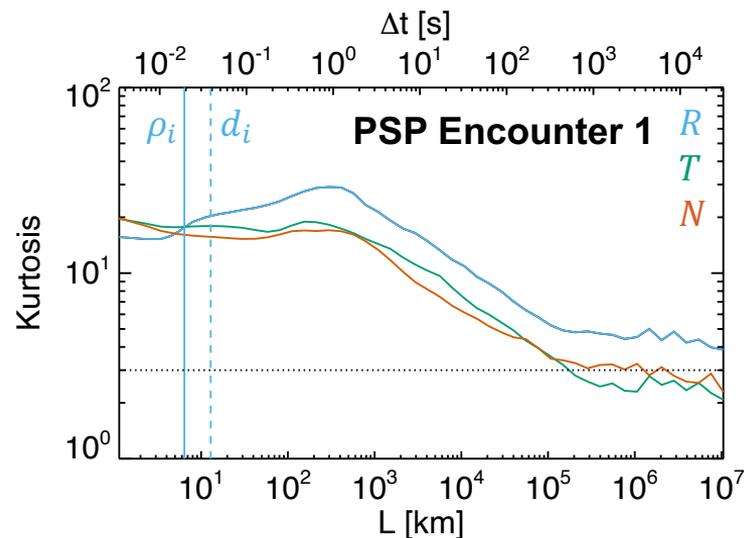
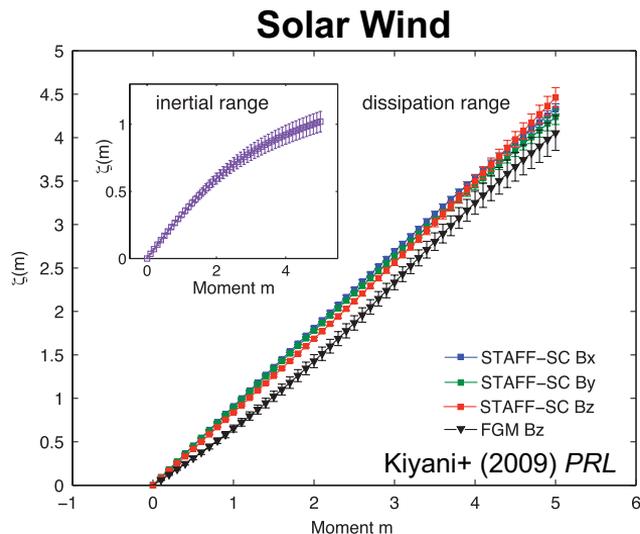
## Scaling of structure functions

$$S_m(\ell) = \left\langle (B_i(x + \ell) - B_i(x))^m \right\rangle \sim \ell^{\zeta(m)}$$

## Scale-dependent kurtosis

$$\frac{S_{4,i}(\ell)}{[S_{2,i}(\ell)]^2} = \frac{\langle [B_i(x + \ell) - B_i(x)]^4 \rangle}{\langle [B_i(x + \ell) - B_i(x)]^2 \rangle^2}$$

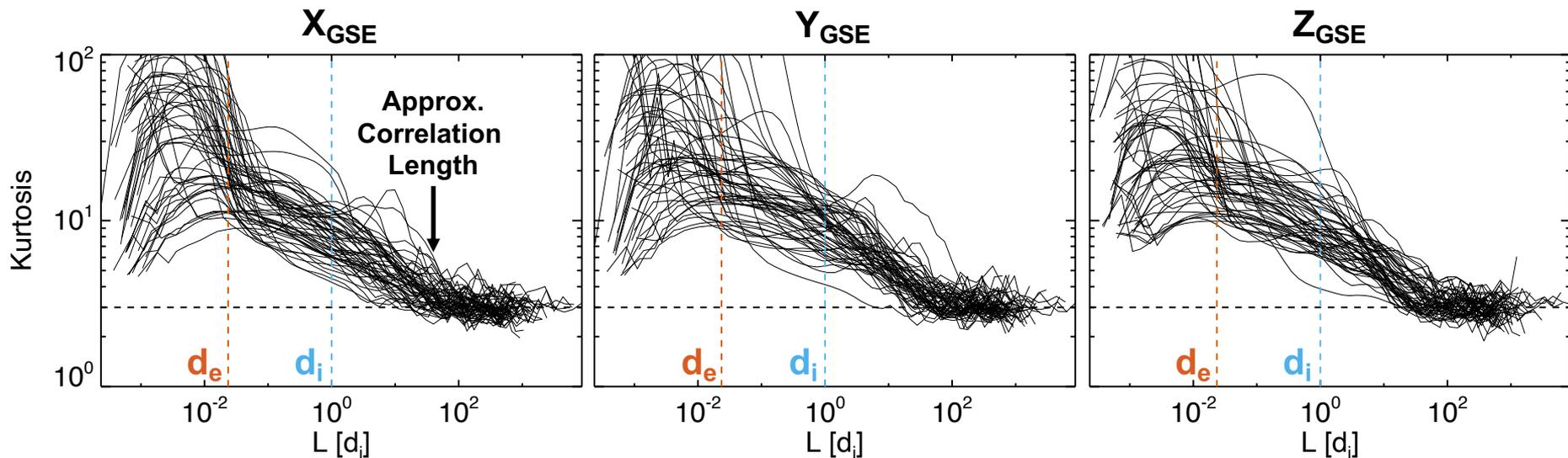
Previous studies show sub-proton scale fluctuations become less intermittent in solar wind



In many cases, the magnetosheath shows increasing scale-dependent kurtosis through sub-proton scales

→ Suggests kinetic scale structures may be different solar wind and magnetosheath

[see also Chhiber+ (2018) *JGR* for a case study]

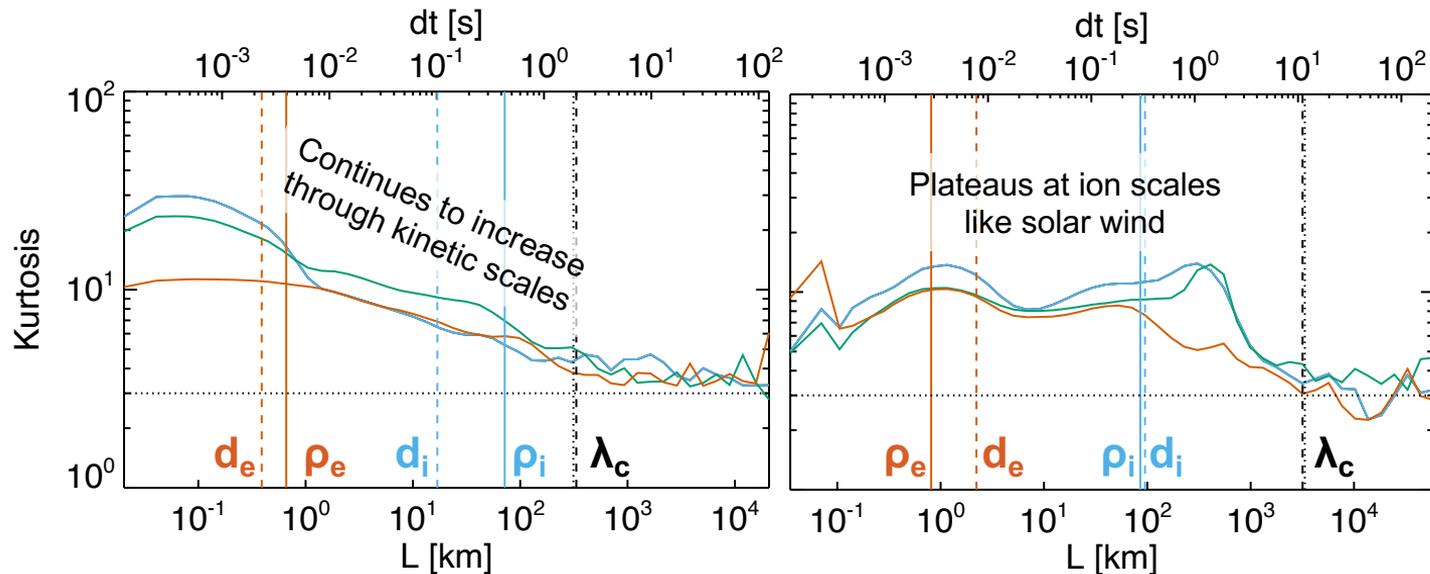


# Scale Dependent Kurtosis

In many cases, the magnetosheath shows increasing scale-dependent kurtosis through sub-proton scales

→ Suggests kinetic scale structures may be different solar wind and magnetosheath

[see also Chhiber+ (2018) *JGR* for a case study]



We examine several properties of the turbulence in the magnetosheath with an eye toward characterizing the similarities and differences with solar wind turbulence

**Taylor Hypothesis** reasonable for many (though not all) magnetosheath intervals and signatures of anisotropy/isotropy scaling with  $\delta b_{rms}/B_0$  apparent

**Correlation Length** in magnetosheath much shorter than those in the solar wind

**Cross Helicity & Residual Energy** place the magnetosheath in a more nonlinear state than many solar wind intervals

**Intermittency** continues to develop through sub-proton scales in many intervals in contrast to solar wind