

# Dissipation in Electron-only Reconnection Events: Insights from Pressure-Strain Interaction

Riddhi Bandyopadhyay

Princeton University

8 April 2021

With collaborators: William H. Matthaeus, Alexandros Chasapis

# Pressure-Strain and Dissipation

$$\partial_t f_\alpha + \mathbf{v} \cdot \nabla f_\alpha + \frac{\mathbf{F}}{m_\alpha} \cdot \nabla_v f_\alpha = 0 \quad \leftarrow \text{Assume Vlasov}$$

Distribution function



$\alpha = \text{proton, electron, ...}$

$$\partial_t \mathcal{E}_\alpha^f + \nabla \cdot (\mathcal{E}_\alpha^f \mathbf{u}_\alpha + \mathbf{P}_\alpha \cdot \mathbf{u}_\alpha) = (\mathbf{P}_\alpha \cdot \nabla) \cdot \mathbf{u}_\alpha + n_\alpha q_\alpha \mathbf{E} \cdot \mathbf{u}_\alpha. \quad (1)$$

$$\partial_t \mathcal{E}_\alpha^{th} + \nabla \cdot (\mathcal{E}_\alpha^{th} \mathbf{u}_\alpha + \mathbf{h}_\alpha) = -(\mathbf{P}_\alpha \cdot \nabla) \cdot \mathbf{u}_\alpha. \quad (2)$$

$$\partial_t \mathcal{E}^m + \frac{c}{4\pi} \nabla \cdot (\mathbf{E} \times \mathbf{B}) = -\mathbf{E} \cdot \mathbf{J} \quad (3)$$

Add internal energy: dissipation

# Why Pi-D?

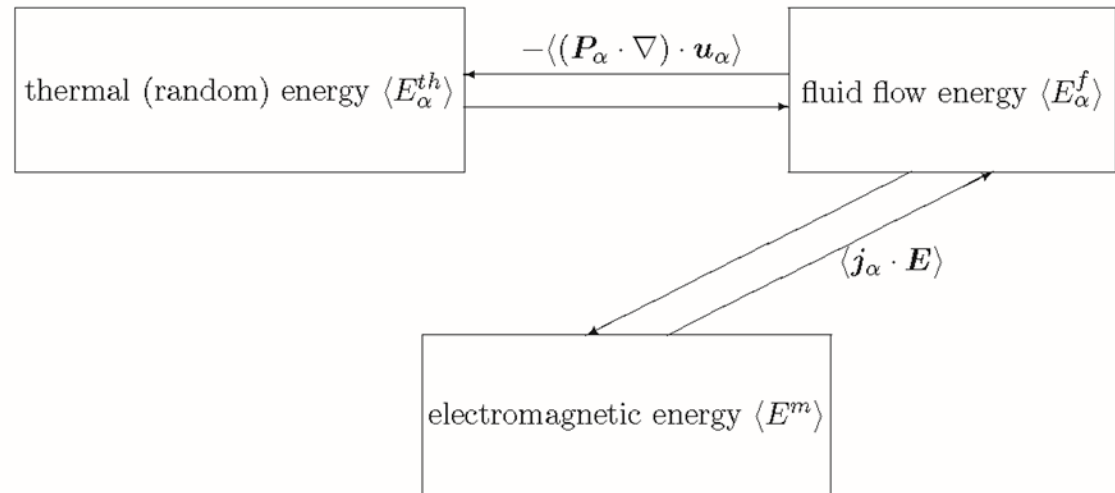
$$\partial_t \langle E_\alpha^f \rangle = \langle (\mathbf{P}_\alpha \cdot \nabla) \cdot \mathbf{u}_\alpha \rangle + \langle n_\alpha q_\alpha \mathbf{E} \cdot \mathbf{u}_\alpha \rangle,$$

$$\partial_t \langle E_\alpha^{th} \rangle = -\langle (\mathbf{P}_\alpha \cdot \nabla) \cdot \mathbf{u}_\alpha \rangle,$$

$$\partial_t \langle E^m \rangle = -\langle \mathbf{E} \cdot \mathbf{j} \rangle.$$

- Pi-D distinguishes ion/electron heating.
- Triangle diagram describes energy conversion.

**$\mathbf{j} \cdot \mathbf{E}$  and Pi-D measure somewhat different stages of energy conversion (dissipation)**



# Pi-D & pθ Decomposition

$$\begin{aligned} -(\mathbf{P} \cdot \nabla) \cdot \mathbf{u} &= -p\delta_{ij}\partial_j u_i - (P_{ij} - p\delta_{ij})\partial_j u_i \\ &= -p\theta - \Pi_{ij}D_{ij}, \end{aligned}$$

Compressive  
heating

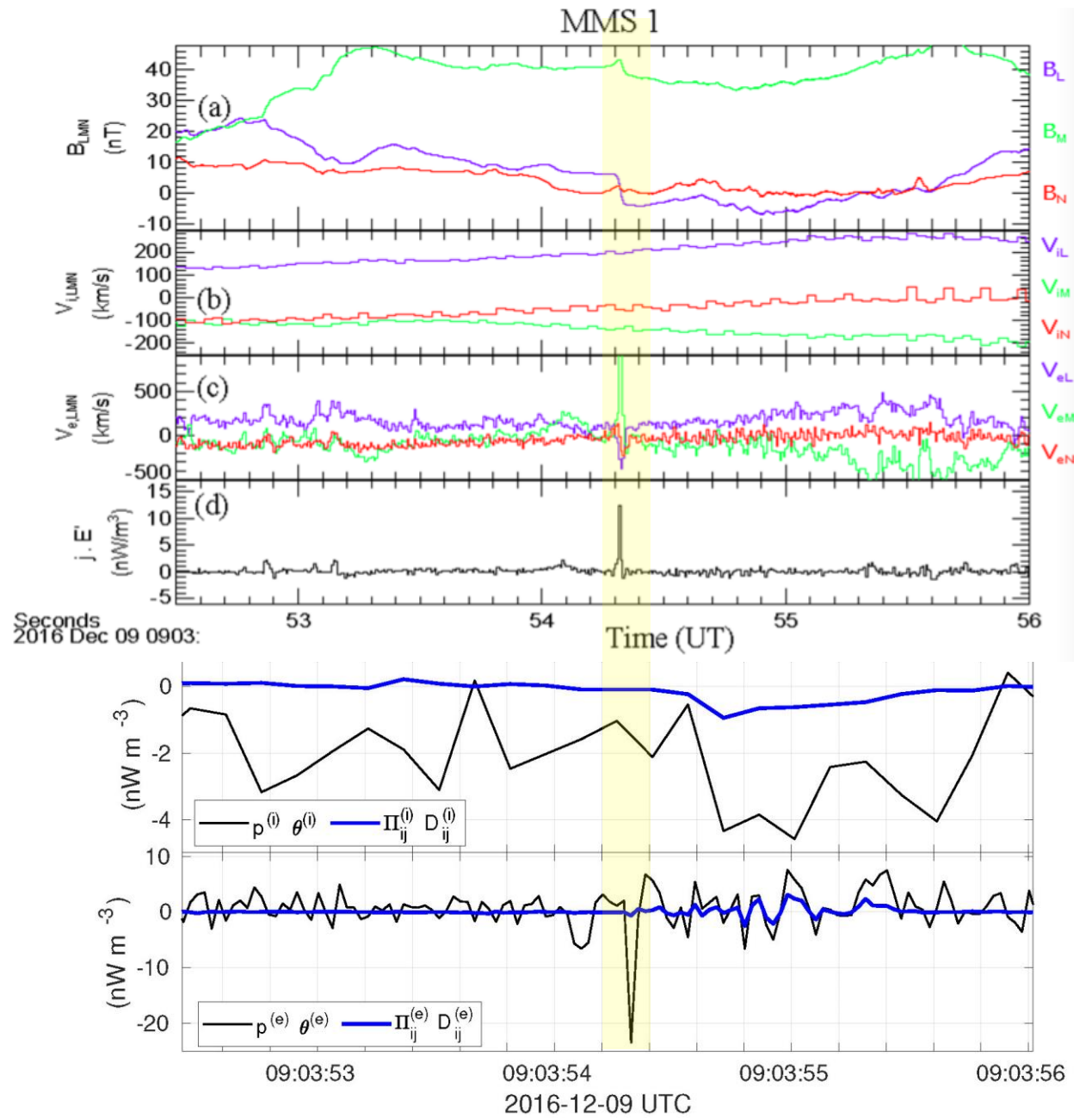
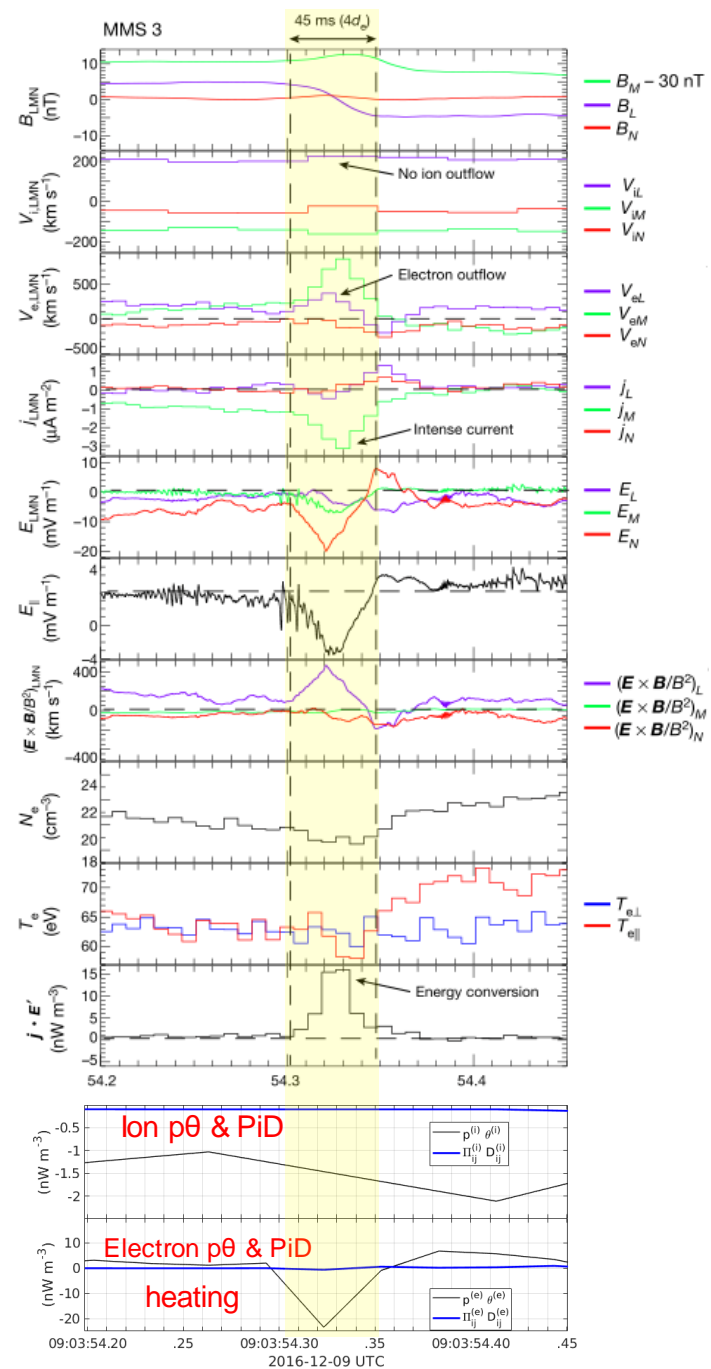
Incompressive  
heating: "Pi-D"

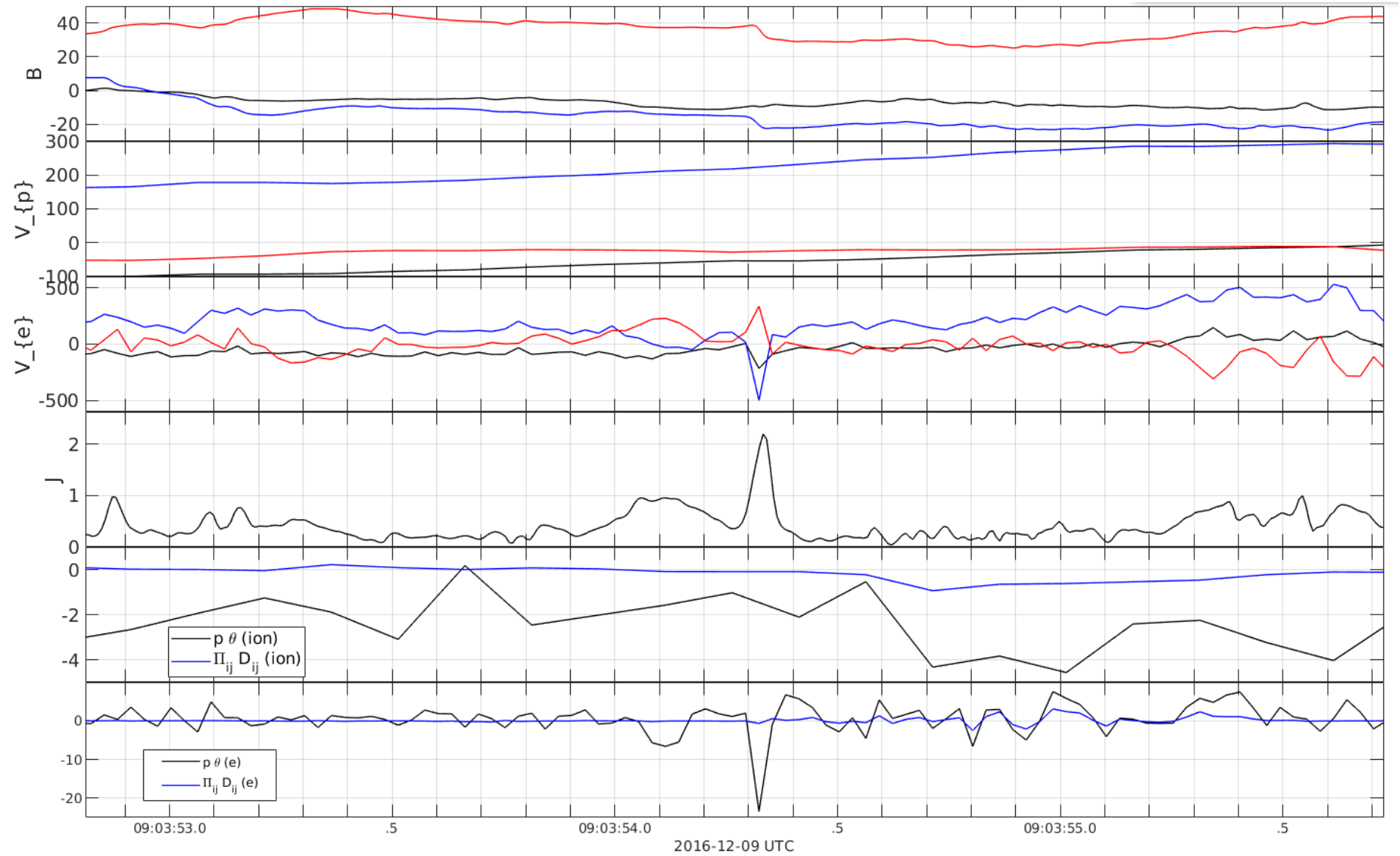
$$p = \frac{1}{3}P_{ii}$$

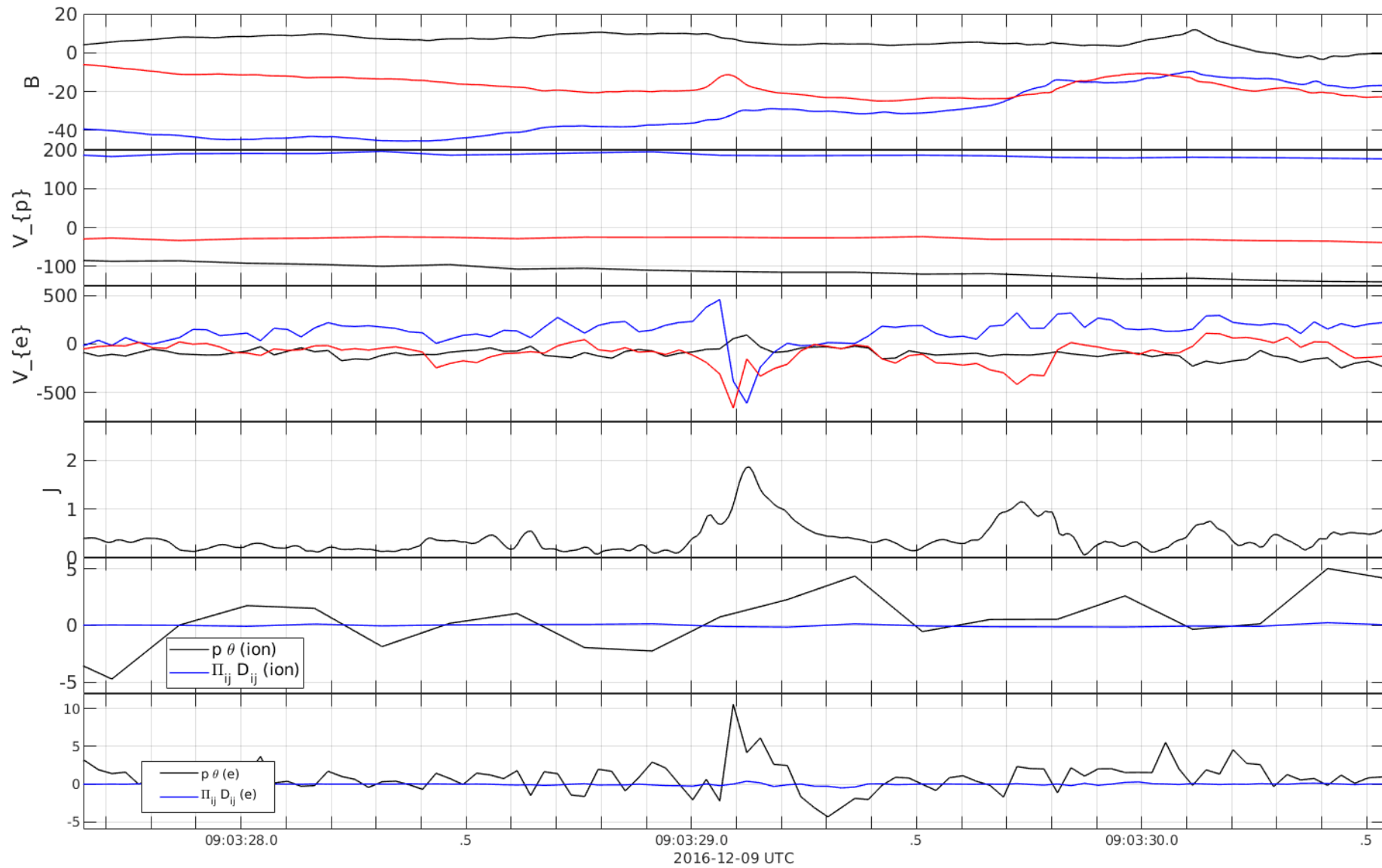
$$\theta = \nabla \cdot \mathbf{u}$$

$$\Pi_{ij} = P_{ij} - p\delta_{ij}$$

$$D_{ij} = \frac{1}{2}(\partial_i u_j + \partial_j u_i) - \frac{1}{3}\theta\delta_{ij}$$







# Summary

- Preliminary analysis shows dominant electron heating.
- Heating via compressive channel.