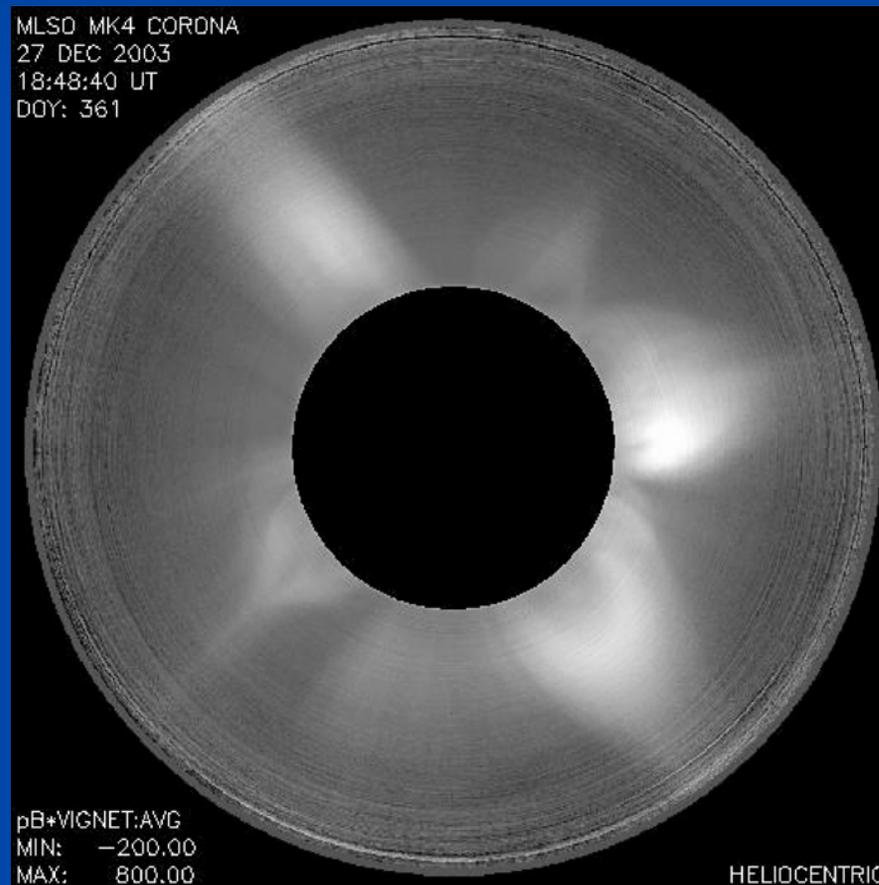


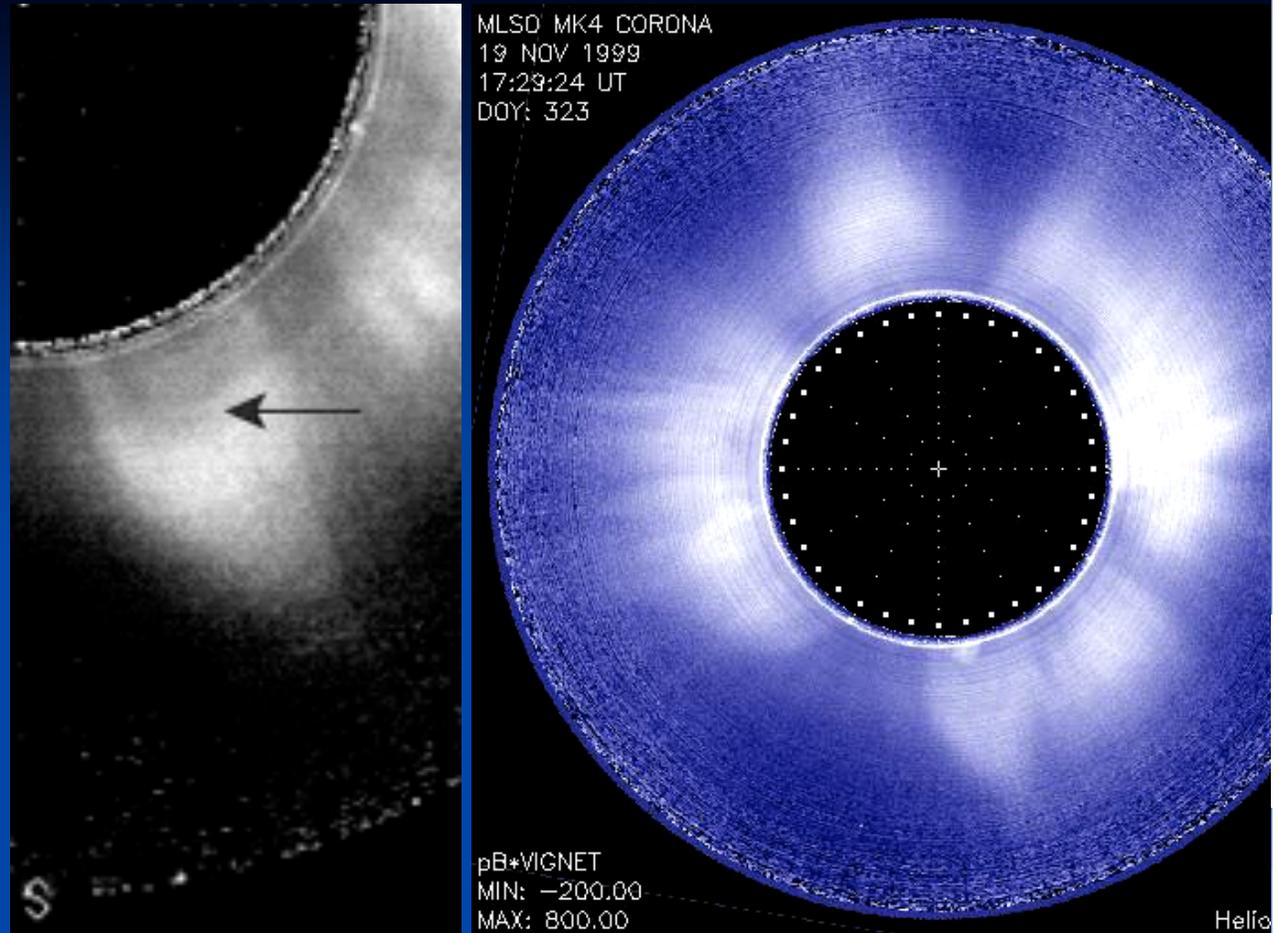
# Observing the Unobservable? Modeling coronal cavities to determine cavity density

Jim Fuller

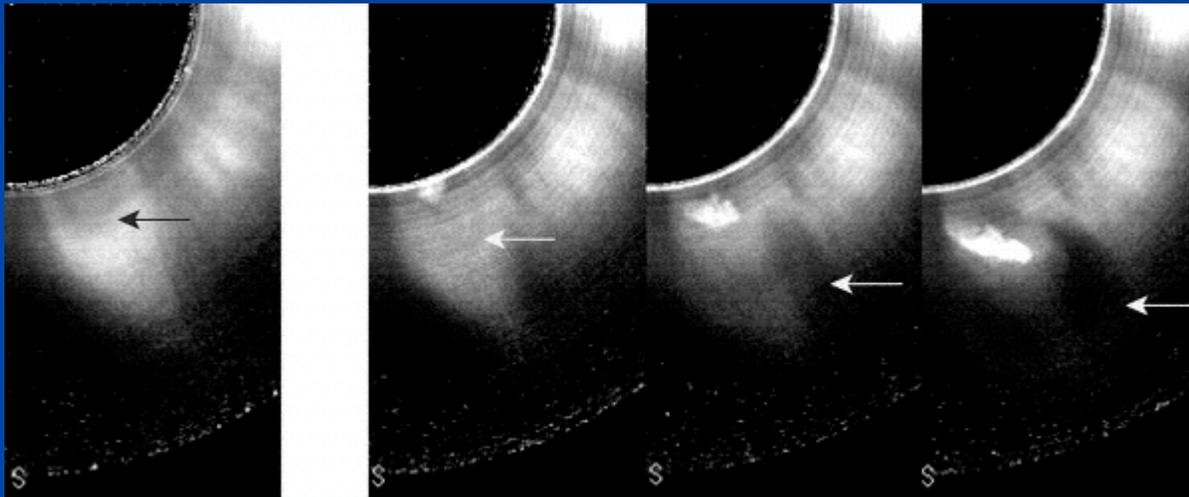


Advisors: Sarah Gibson, Julianna de Toma

# Motivations



- Cavities are known to be correlated with coronal mass ejections
- Understanding the physics of cavities is essential to understanding and predicting phenomena such as CMEs



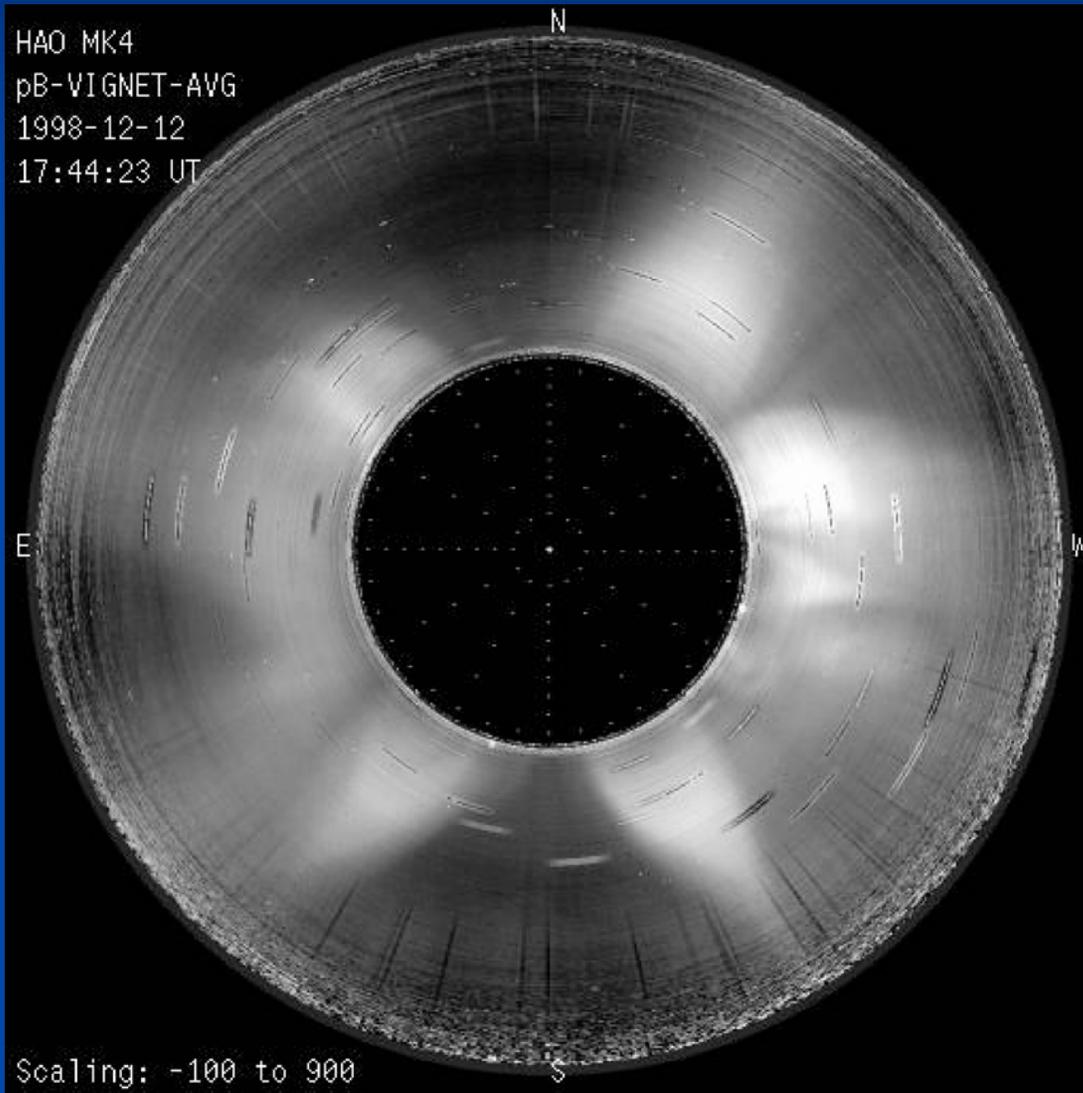
# Background

- Cavities are regions with lower density located at the base of coronal helmet streamers
- Cavities are associated with CMEs
- Lower cavity density may imply stored magnetic energy within cavity
- Cavities are often long-term structures

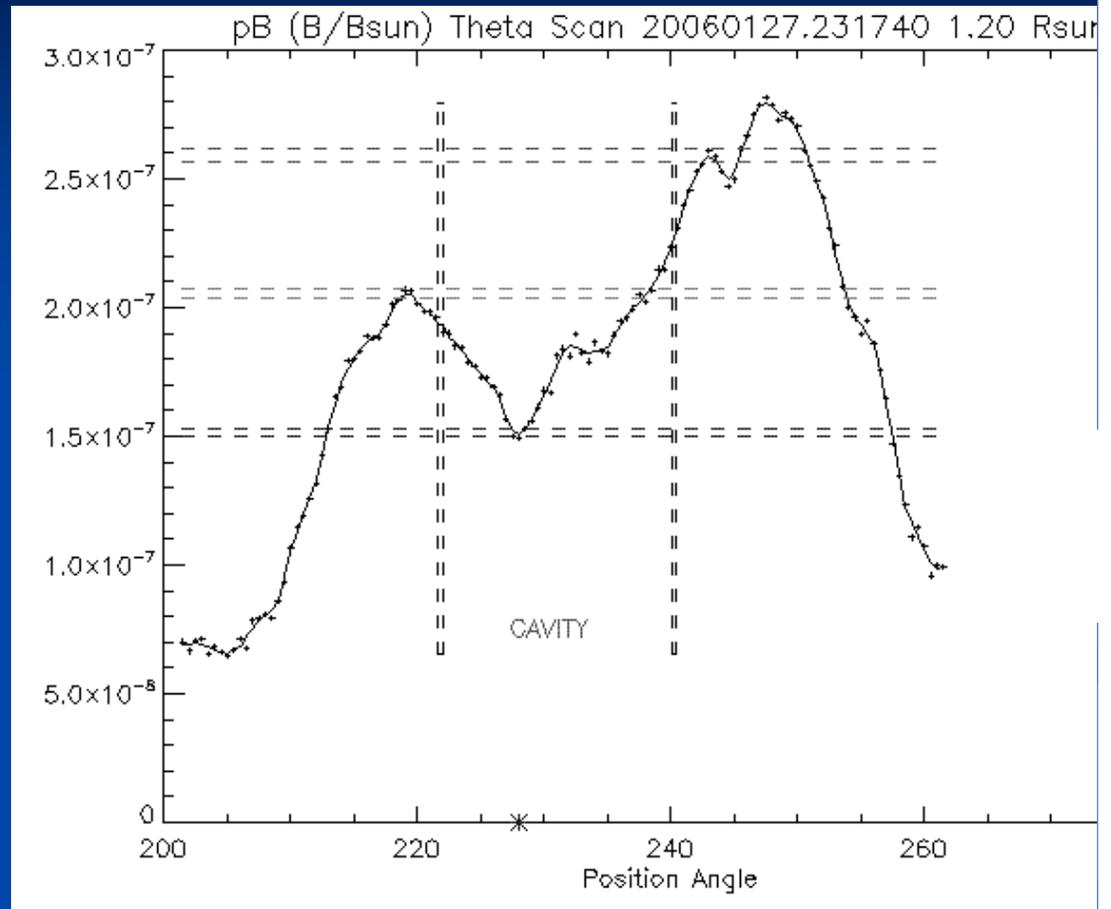
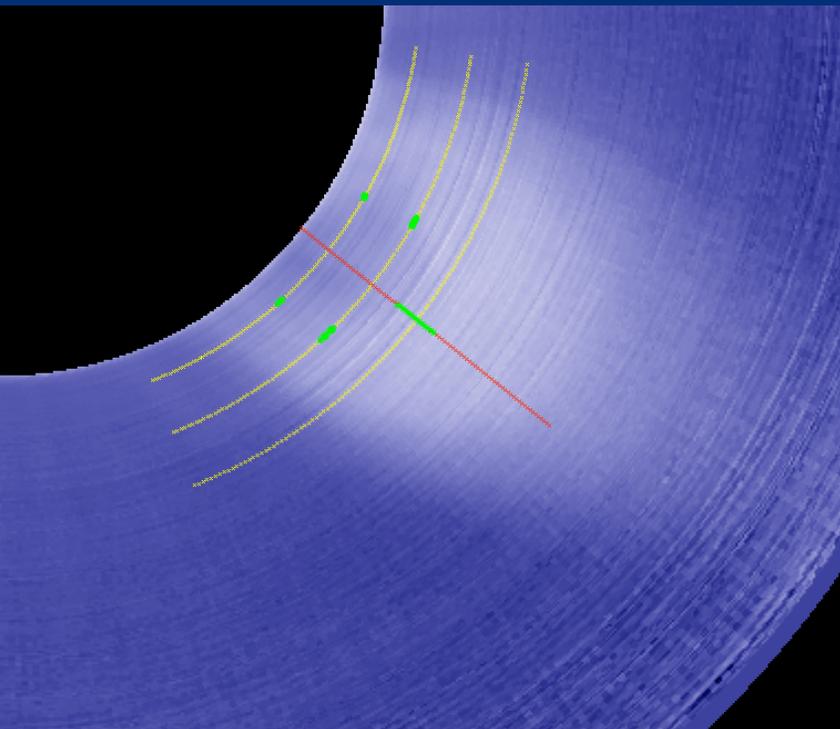
# Goals of project

- Create a cavity model that will allow us to observe cavity material
- Find cavities that fit parameters of model so we can claim we are observing only cavity material
- Invert polarized brightness measurements to determine cavity density

# Observing a Cavity



- Each pixel brightness is an integral over the line of sight, integral is proportional to density
- Cavity wall, other features often get in way
- 2D image cannot tell 3D structure so we must observe for several days

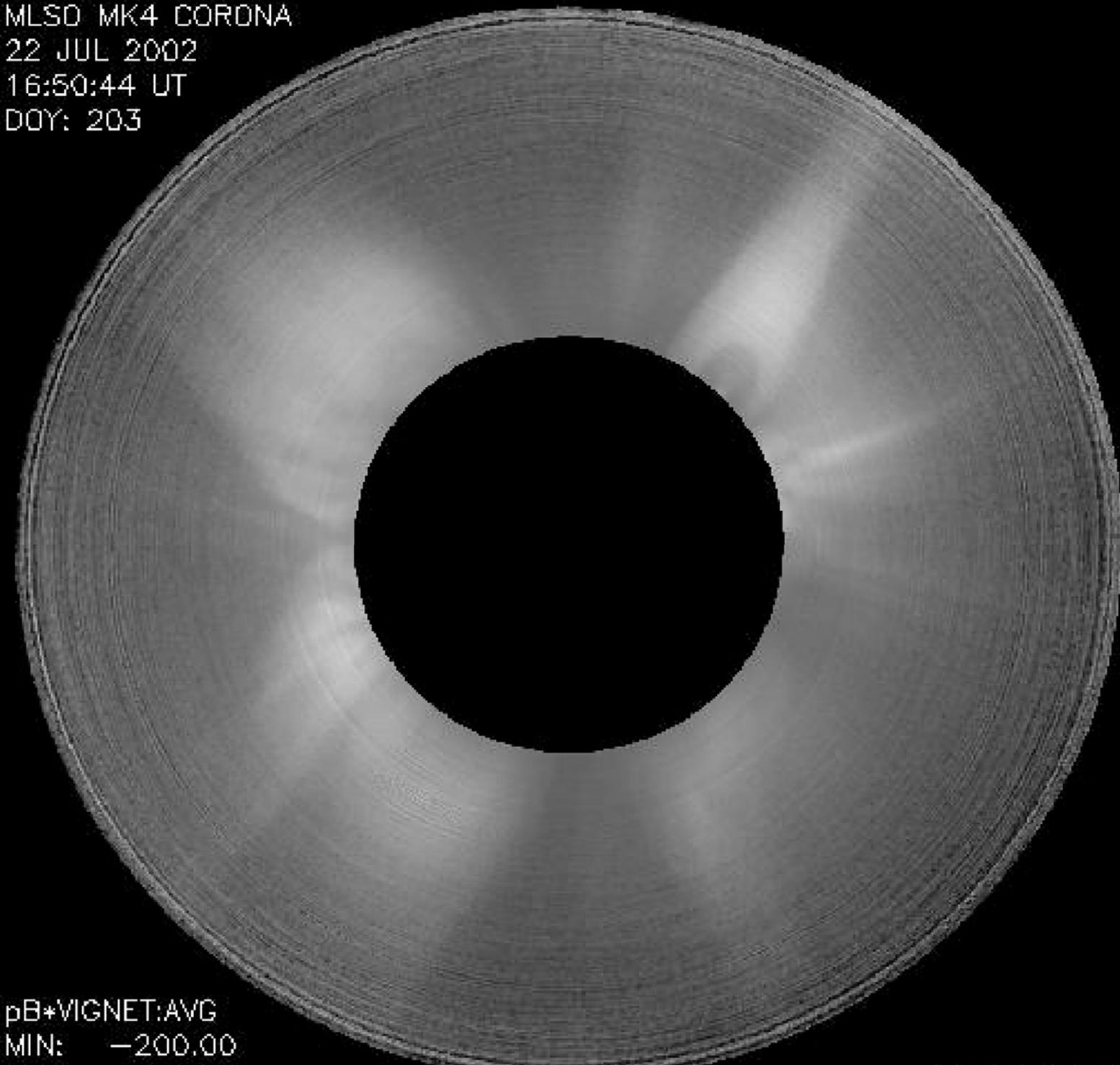


- Polarized brightness measurements as a function of latitude at constant height
- Cavity has lower brightness than rim, higher brightness than coronal holes

# Our Model

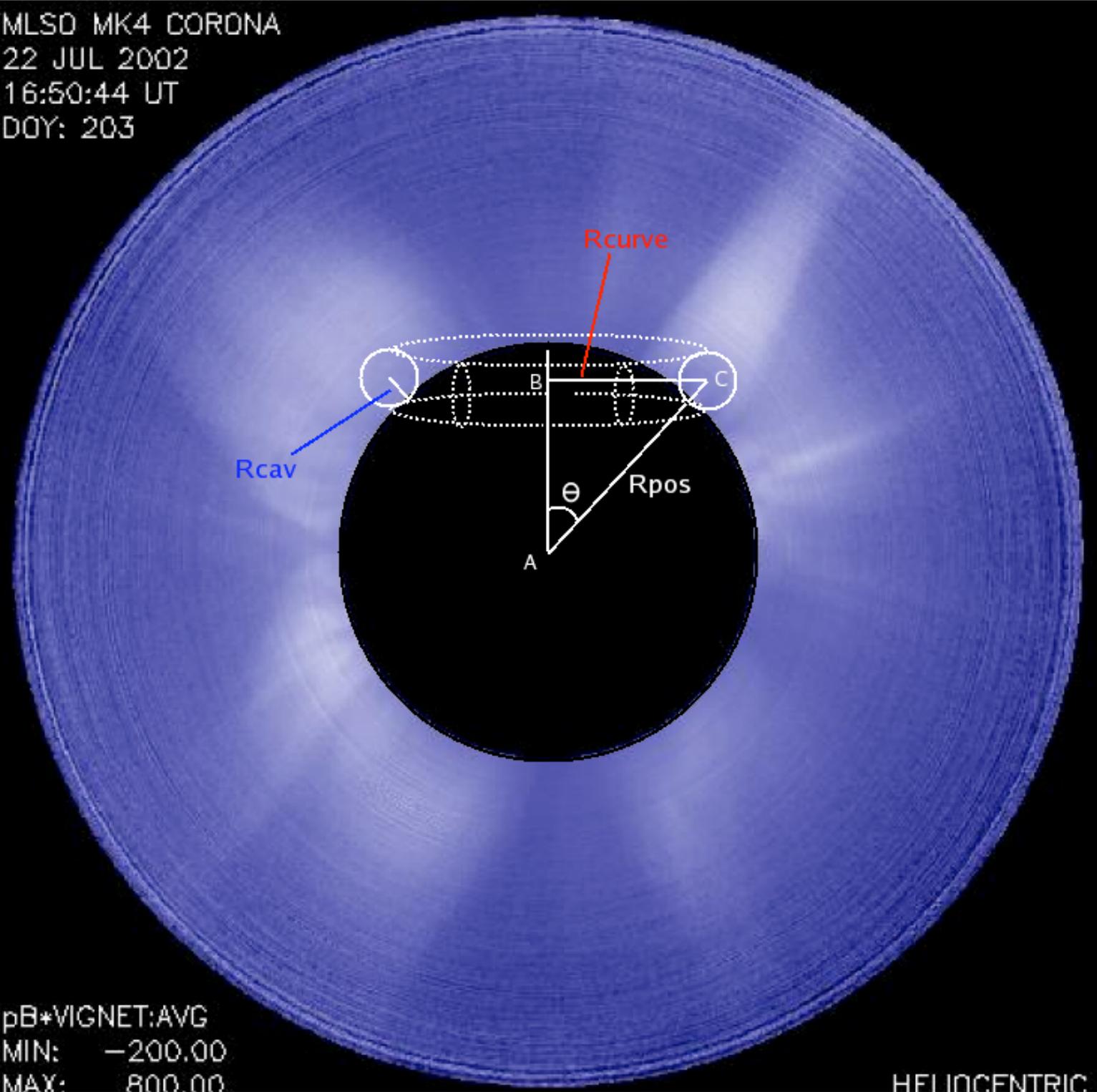
- Cavity is modeled as an axisymmetric torus encircling Sun at constant latitude.
- The model is not intended to apply to all cavities but will work if cavity has the right properties
- Cavity must maintain constant size and latitude for several days
- Cavity must be large and at low latitudes
- These cavities will allow density analysis

MLSD MK4 CORONA  
22 JUL 2002  
16:50:44 UT  
DOY: 203



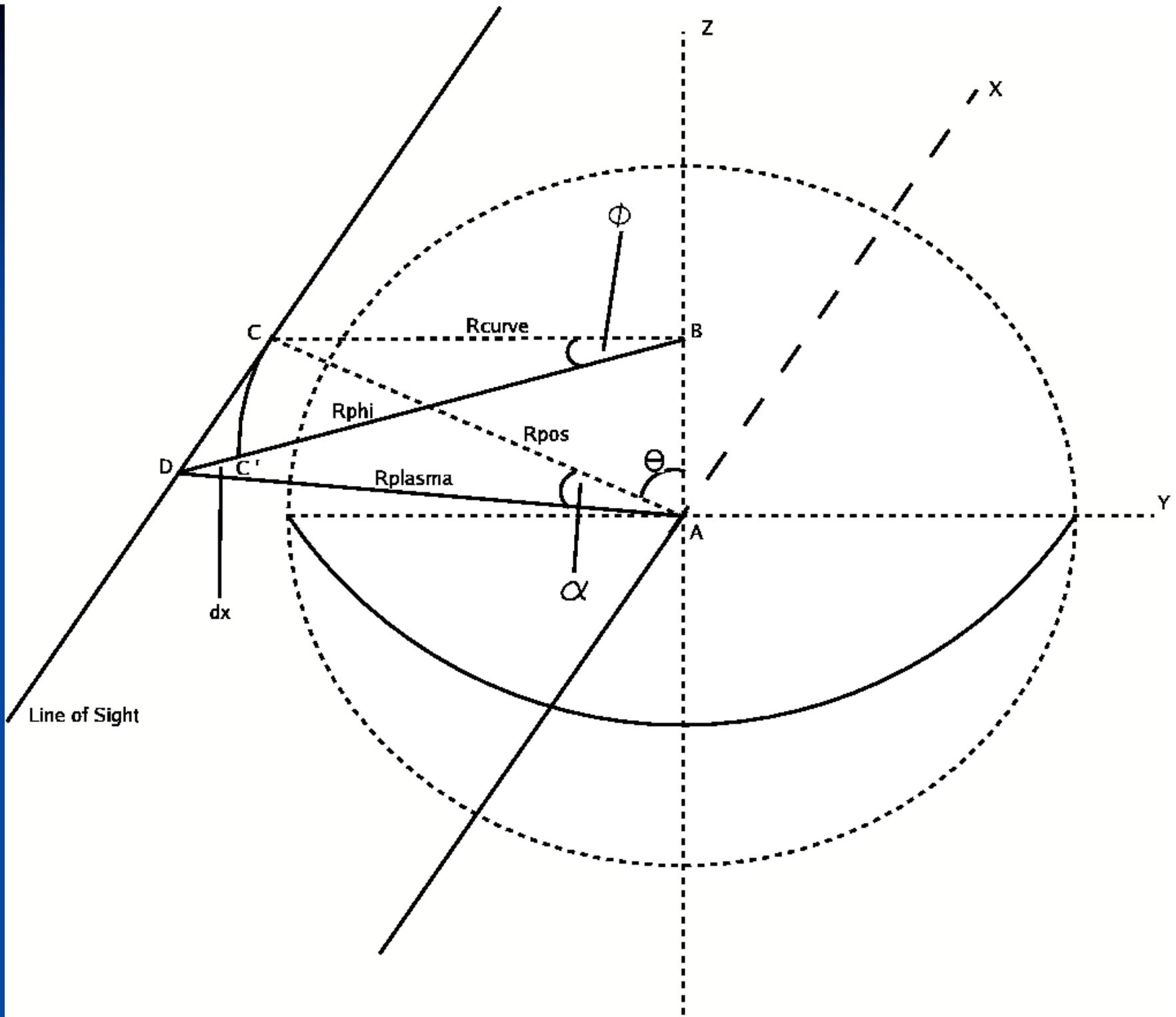
pB\*VIGNET:AVG  
MIN: -200.00

MLSD MK4 CORONA  
22 JUL 2002  
16:50:44 UT  
DOY: 203

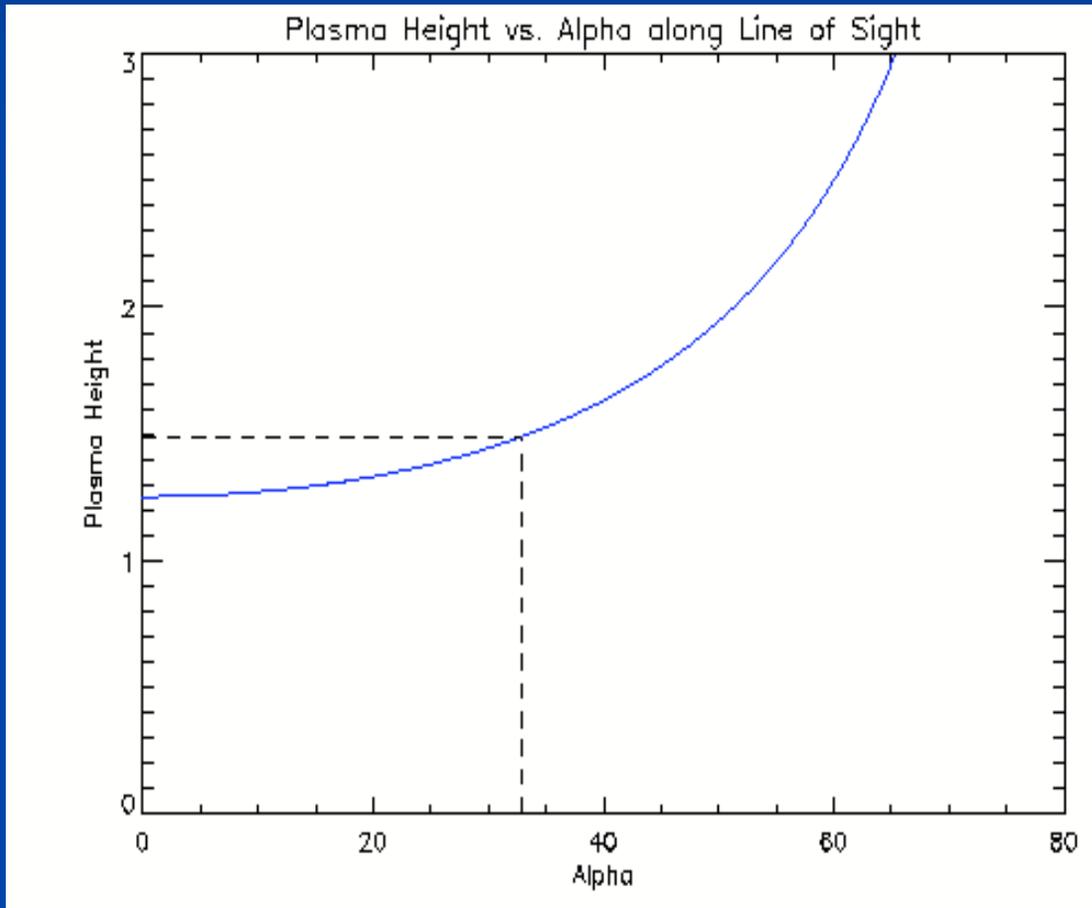


pB\*VIGNET:AVG  
MIN: -200.00  
MAX: 800.00

HELIOCENTRIC



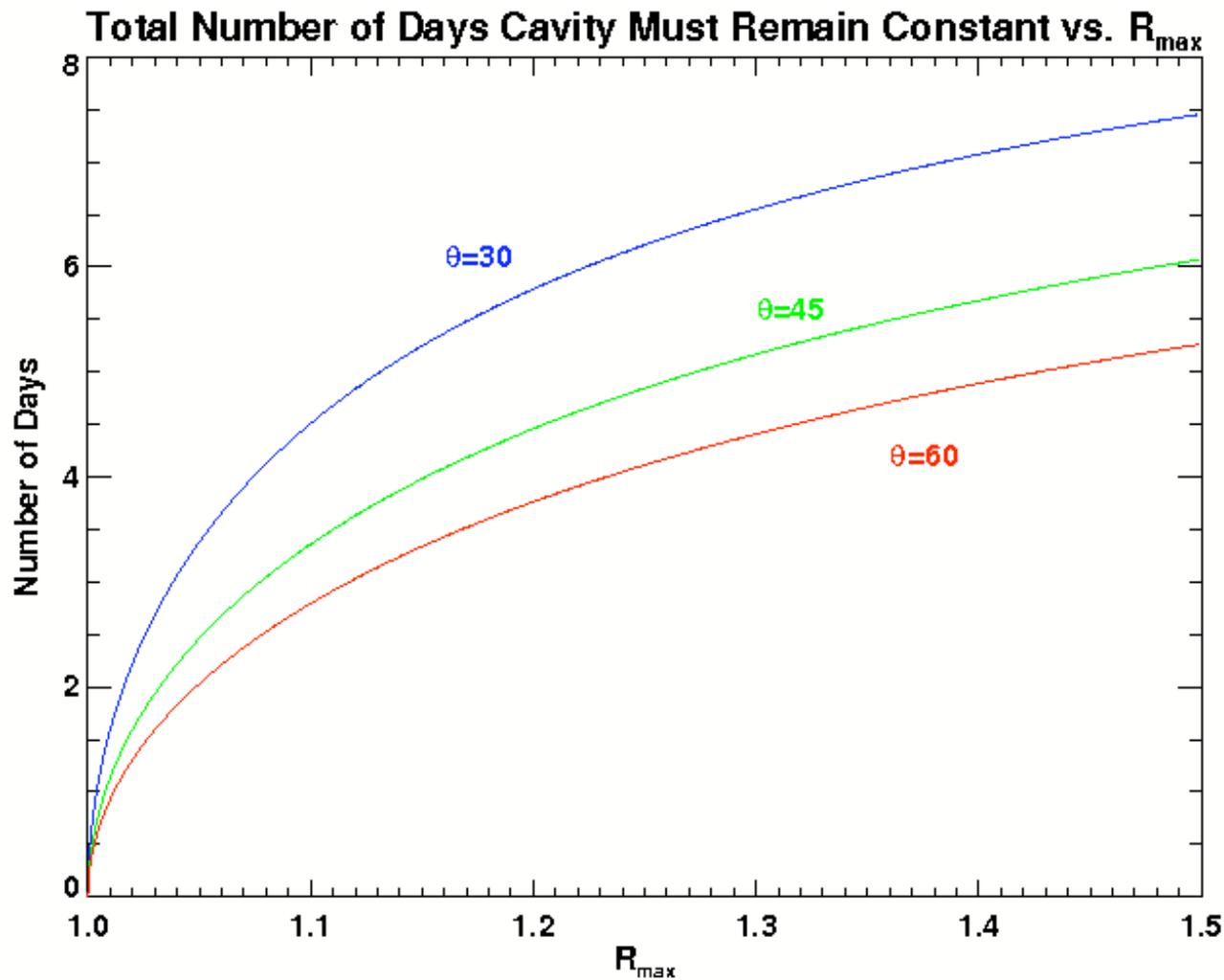
# Geometry of Cavity Along Line of Sight of Sight



- Material from altitudes higher than  $R_{pos}$  projects into line of sight as scattering angle increases
- Material from altitudes below  $R_{pos}$  can never project into line of sight

# Limitations on Observable Cavities

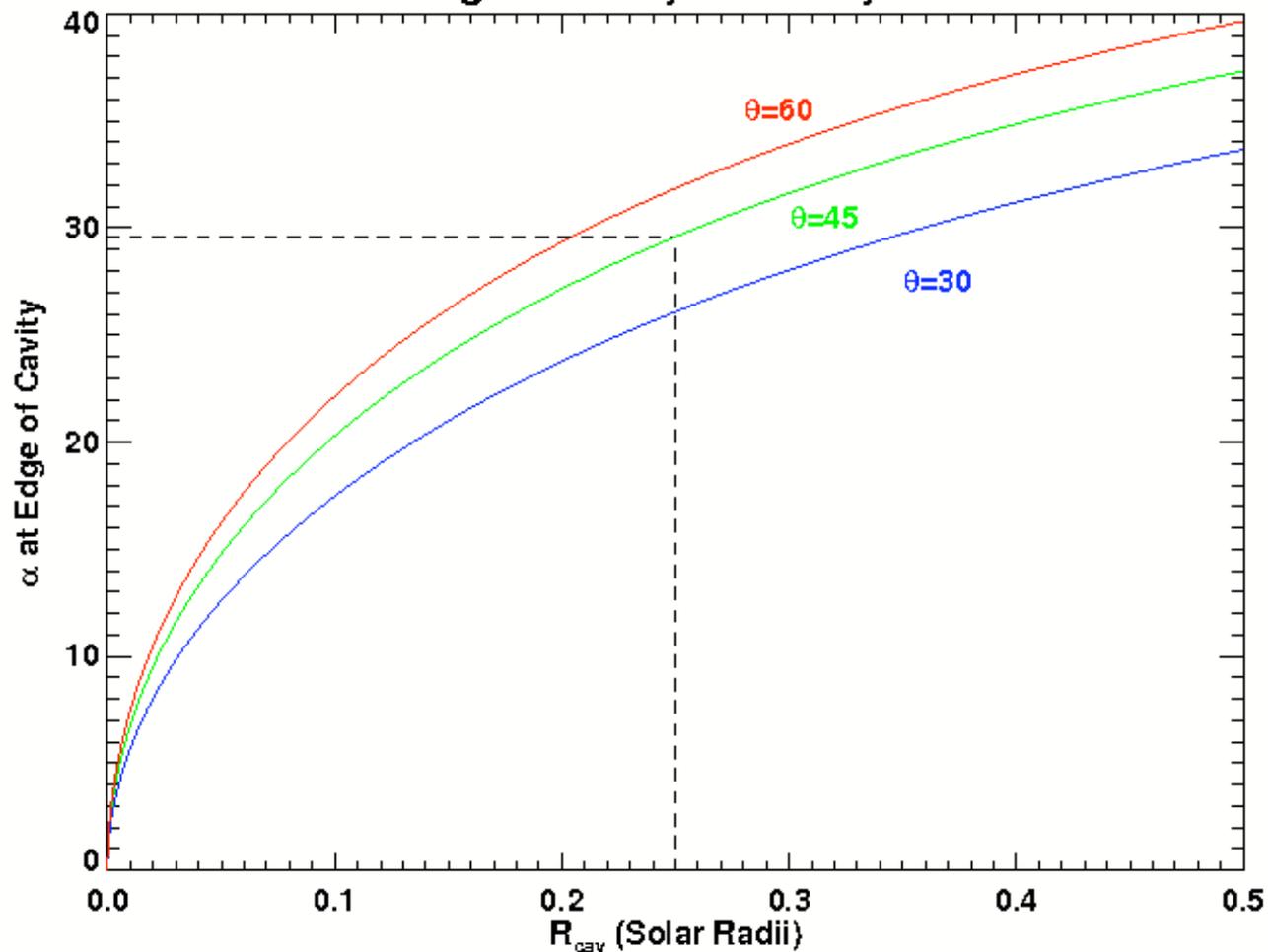
- Bigger cavities are easier to observe because they extend to larger heights
- Cavities near equator are easier to observe because they curve less
- Cavity must also be visible a couple days before and after observation in order to prove it has large enough longitudinal extent



- In order to fit our model, a cavity must be large enough of a donut that it is axisymmetric along our line of sight
- The size of the donut slice can be measured by observing how many days a cavity is visible

■ This plot tells us the total number of days a cavity must be visible that the cavity fits our model and is suitable for observation on the middle day

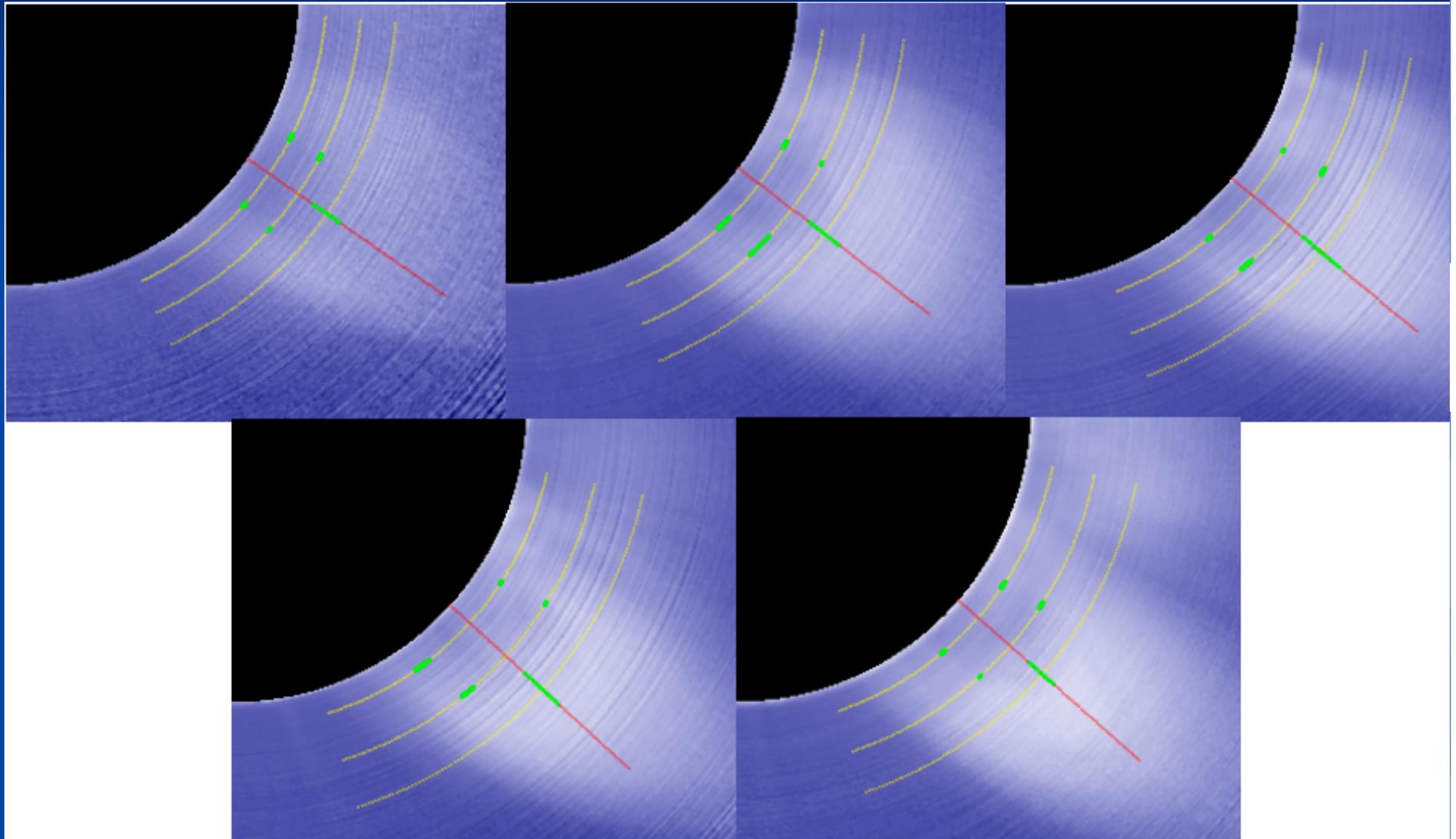
$\alpha$  at Edge of Cavity vs. Cavity Radius



- Assuming cavity is axisymmetric, a big cavity is best for observation
- Scattering angle at edge of cavity is large for bigger cavities
- This means that most light comes from within the cavity as opposed to outside it

- Scattering angle at edge of cavity also dependent on  $R_{pos}$
- Lines of sight at low altitudes yield higher scattering angle

# Our Cavity



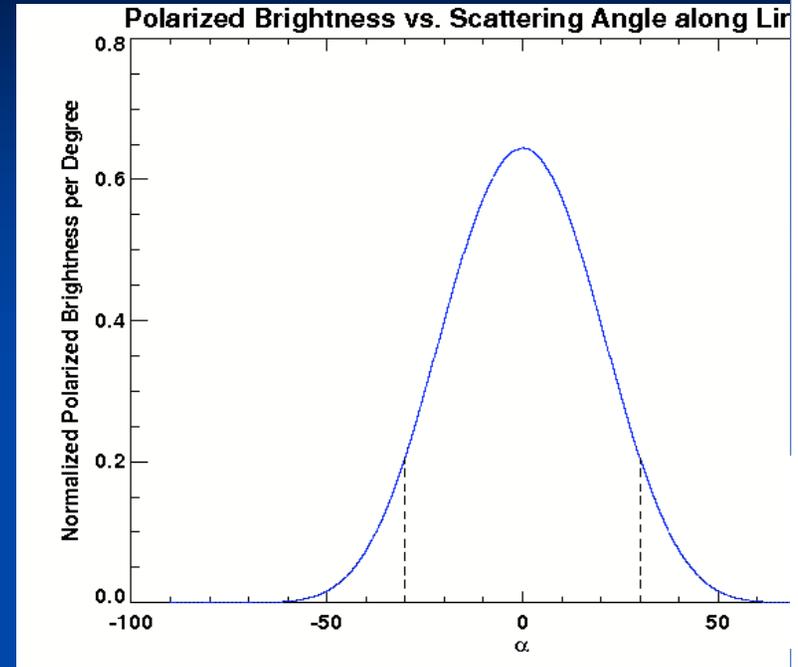
# What date works best for measurements

Date	Days Required	Days Observed
01/25/06	$2.50^{+0.11}_{-0.13}$	0 before, 5 after
01/27/06	$2.66^{+0.13}_{-0.13}$	2 before, 3 after
01/28/06	$2.71^{+0.14}_{-0.17}$	3 before, 2 after
01/29/06	$2.80^{+0.14}_{-0.17}$	4 before, 1 after
01/30/06	$2.70^{+0.10}_{-0.13}$	5 before, 0 after

Our cavity is almost axisymmetric on the 27<sup>th</sup> and 28th

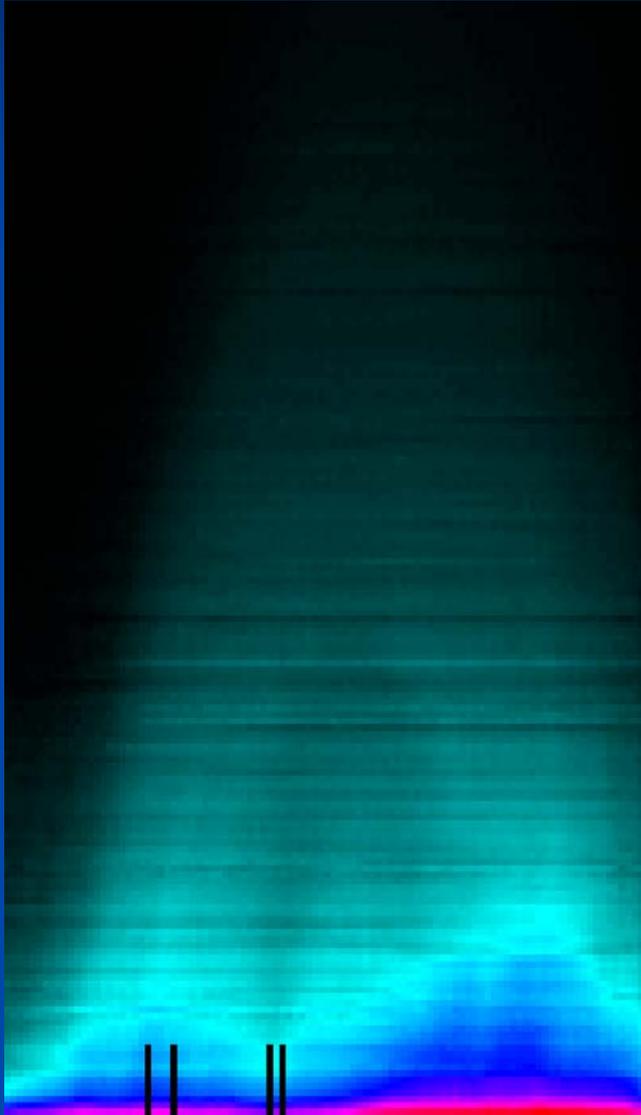
# Cavity Properties

Date	$R_{cav}$	$\theta$	$\alpha_{max}$
01/25/06	$.230 \pm .030$	$124.80 \pm .74$	$30.32^{+1.48}_{-1.65}$
01/27/06	$.260 \pm .035$	$128.44 \pm .63$	$31.17^{+1.53}_{-1.71}$
01/28/06	$.270 \pm .045$	$129.64 \pm .67$	$31.40^{+1.85}_{-2.14}$
01/29/06	$.285 \pm .045$	$132.40 \pm .89$	$31.54^{+1.81}_{-2.07}$
01/30/06	$.260 \pm .030$	$131.36 \pm .54$	$30.69^{+1.33}_{-1.45}$



- Cavity is big and fairly close to the equator so  $\alpha_{max}$  is large
- Plot at right (Hundhausen 1993) shows polarized brightness as function of  $\alpha$  for  $R_{pos}=1.25$
- Over 88% of light comes from within our cavity if we observe it  $R_{pos}=1.25$

# Calculating Cavity Density



Step 1:

- Select regions at which to make radial polarized brightness measurements
- Heights below 1.18 contaminated by substructure
- Heights above 1.4 measure very little cavity
- Beware of active regions!

# Problem

- Van de Hulst inversion requires cylindrical symmetry of density fall off, i.e. the radial fall off must be identical at all scattering angles
- Jump in density from cavity to cavity rim breaks this symmetry

# Uncertainties

- Inversion requires value:

$$pB_{cav}|_{-90}^{90} = 2pB_{cav}|_{\alpha_{max}}^{90} + 2pB_{cav}|_0^{\alpha_{max}}$$

- The measured value is:

$$pB_{meas} = pB_{cav} + pB_{non} = 2pB_{cav}|_0^{\alpha_{max}} + 2pB_{non}|_{\alpha_{max}}^{90}$$

- The value given to our program is:

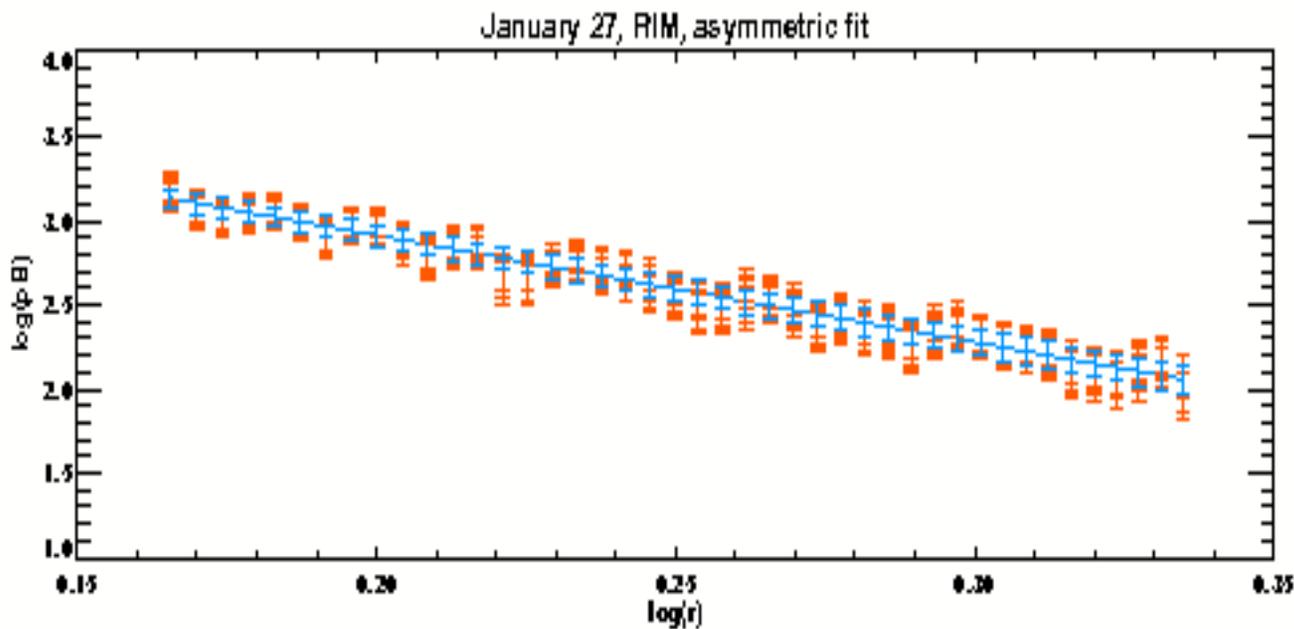
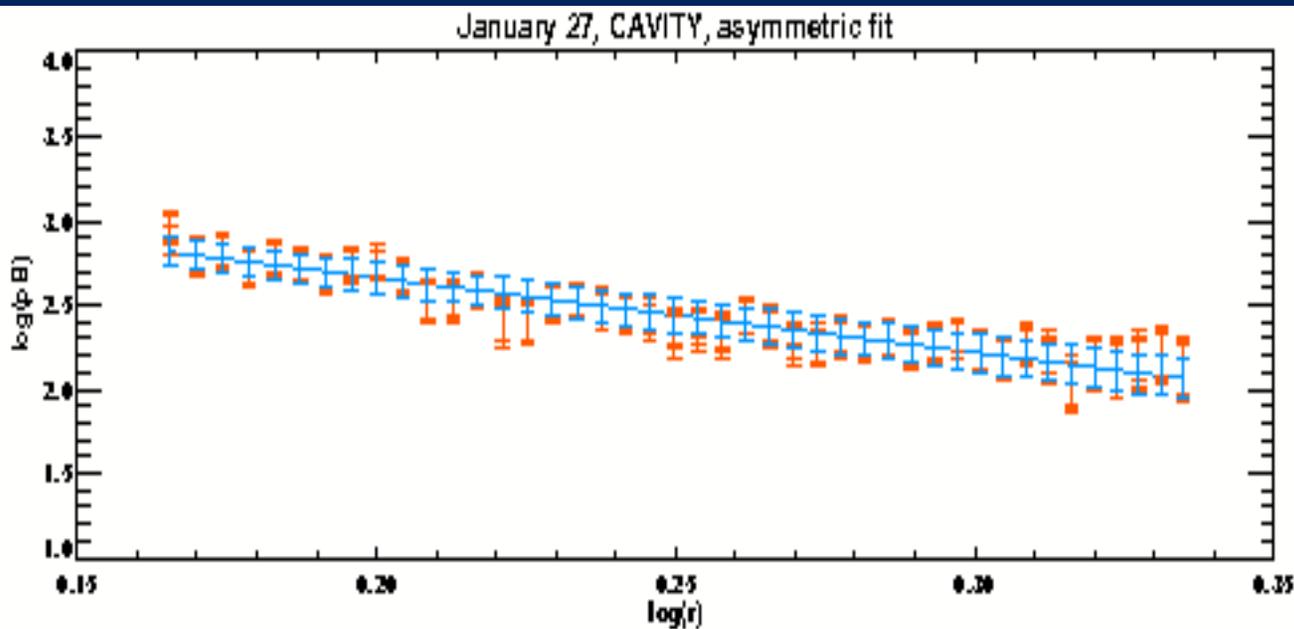
$$pB_{cav}|_{-90}^{90} = pB_{meas} + \left( 2pB_{cav}|_{\alpha_{max}}^{90} - 2pB_{non}|_{\alpha_{max}}^{90} \right)$$

where the term in parentheses is the uncertainty in measurement

# Another Problem

- Cavity is not quite axisymmetric
- Using number of days before and after observation, we calculate values of  $\alpha_{\max}$  in front of and behind cavity at which line of sight exits cavity
- Uncertainties utilize smallest values of  $\alpha_{\max}$  to ensure account for largest possible error

# Fitting a curve to pB measurements



Step 2:

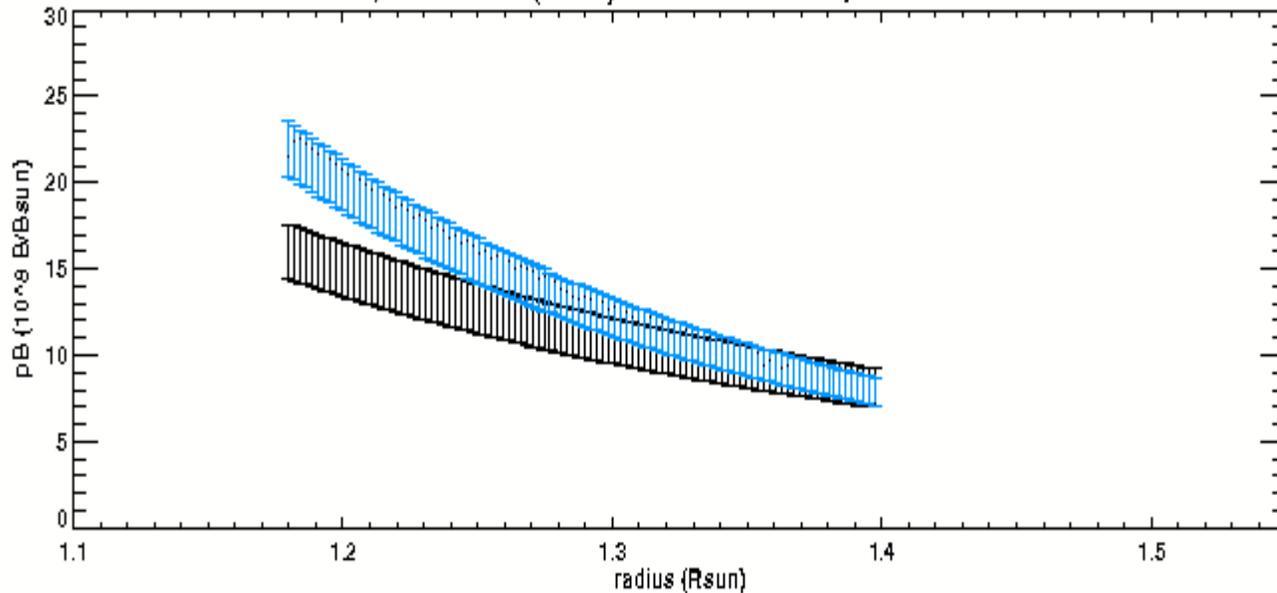
- Create  $\log(pB)$   $\log(r)$  plot
- Log-log plot has linear profile
- Our program determines parameters of line of best fit

# Calculating Cavity Density

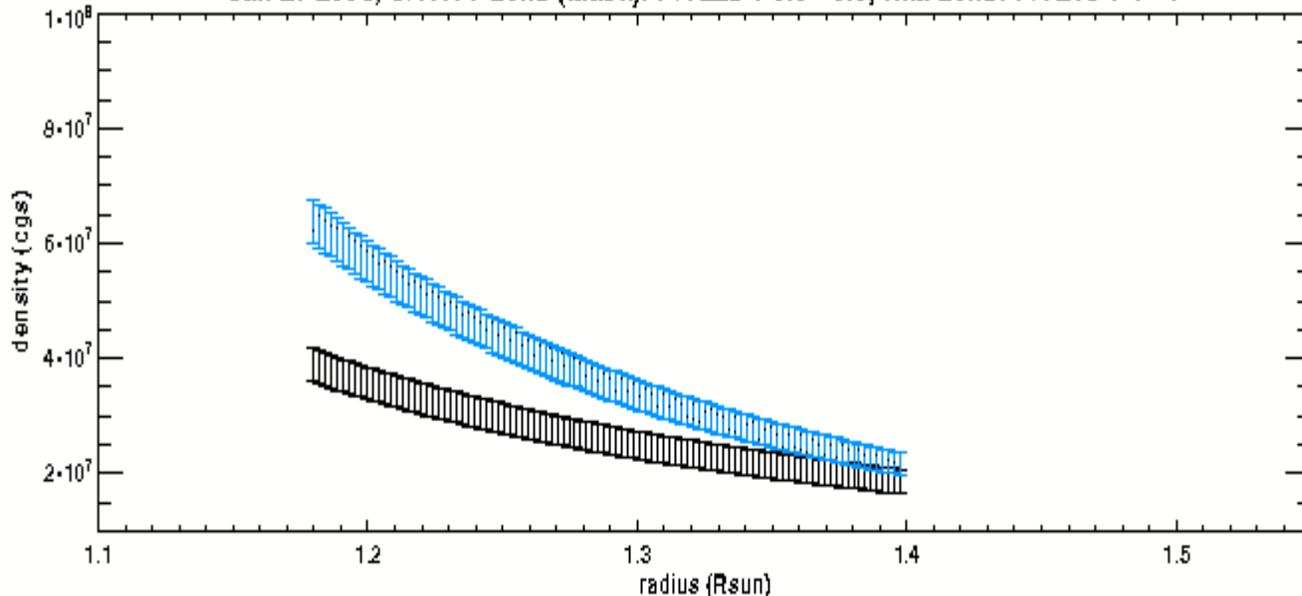
Step 3:

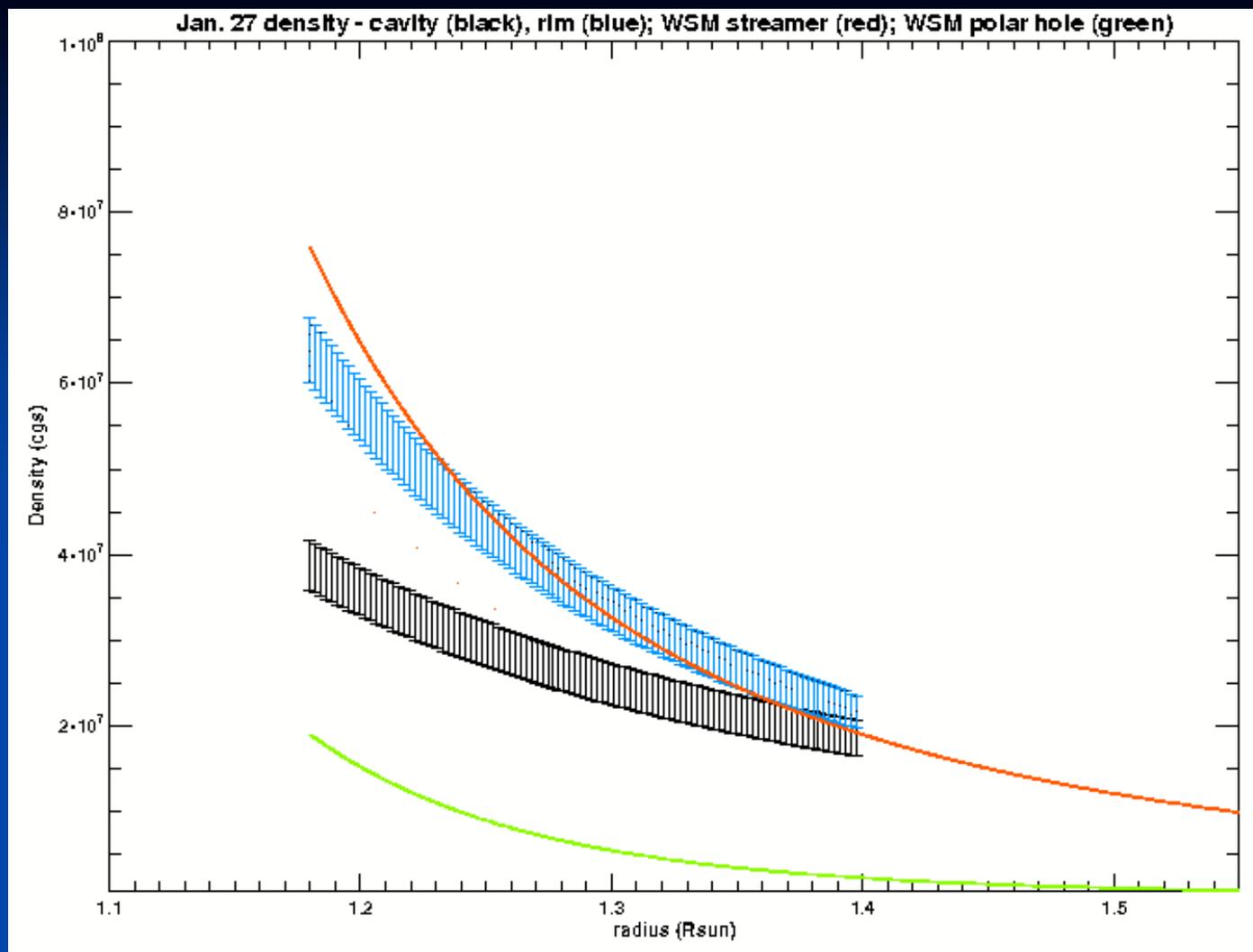
Using calculated  
fit parameters  
perform Van  
Hulst inversion  
and calculate  
density profile

Jan 27 2006, CAVITY PB (black): PA 228 + 0.5 - 0.5; RIM PB: PA 219 + 1 - 1



Jan 27 2006, CAVITY dens (black): PA 228 + 0.5 - 0.5; RIM dens: PA 219 + 1 - 1





- Cavity has about 60-100% the density of the cavity rim
- Cavity has about 2-5 times the density of a coronal hole
- Cavity rim has very similar density to a bright helmet streamer

# Implications

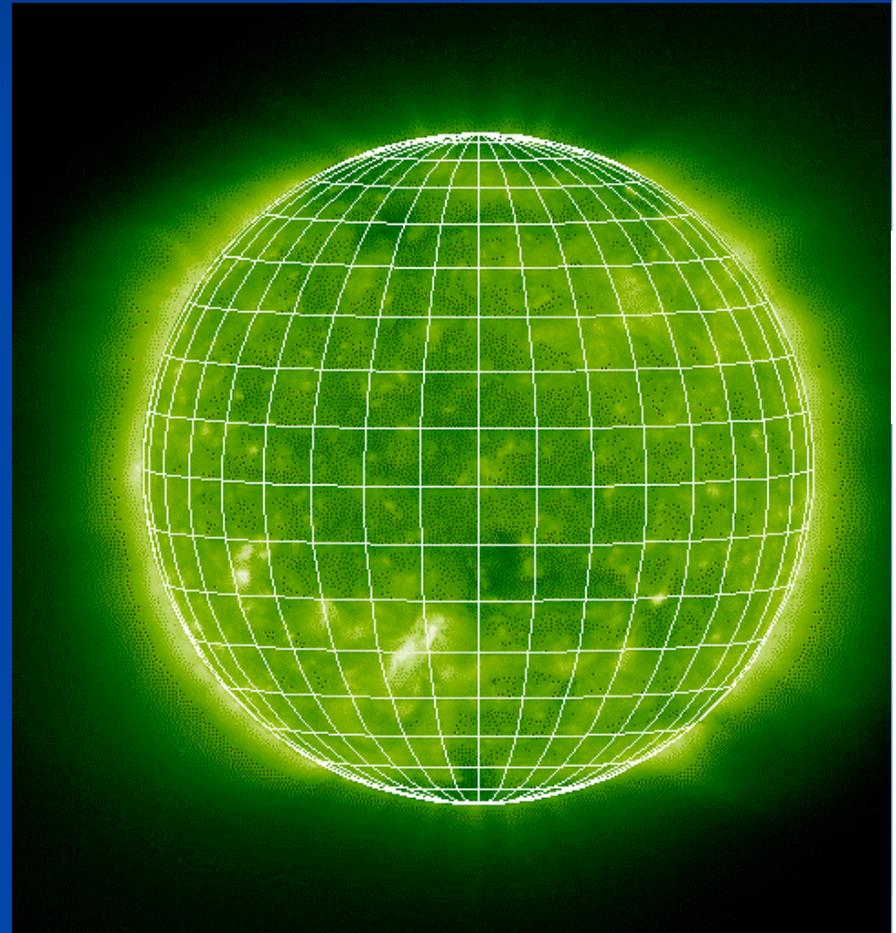
- Cavity has lower density than rim and slower density fall off
- To ensure pressure continuity, cavity must have higher temperature or higher magnetic pressure
- Our results are consistent with models in which cavity is created by twisted magnetic flux rope
- Twisted magnetic flux rope would create a higher magnetic pressure and flatter density fall off within cavity

# Conclusions

- People have said that cavities are unobservable because the helmet streamer gets in the way and because cavities are empty
- We have demonstrated cases in which contribution from the helmet streamer are negligible and have proven that cavities are far from empty
- Our results reveal a density profile that is consistent with the magnetic flux rope model for cavities

# Future Work

- Apply this technique to more cavities
- Apply geometry of the model to cavities imaged in emission lines
- Submit article for publishing
- Use emission line data to determine temperature profiles of cavities



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- Van de Hulst, H.C. 1950, Bulletin of the Astronomical Institutes of the Netherlands, 11, 135