



NORTH CAROLINA STATE UNIVERSITY

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# Off Equatorial Analysis of Several Commonly Used Magnetic Field Models

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O'Brien

# Goals

- Evaluate various external magnetic field models included in the ONERA-DESP code above and below the equatorial plane
- Recommend appropriate potential model validity situations

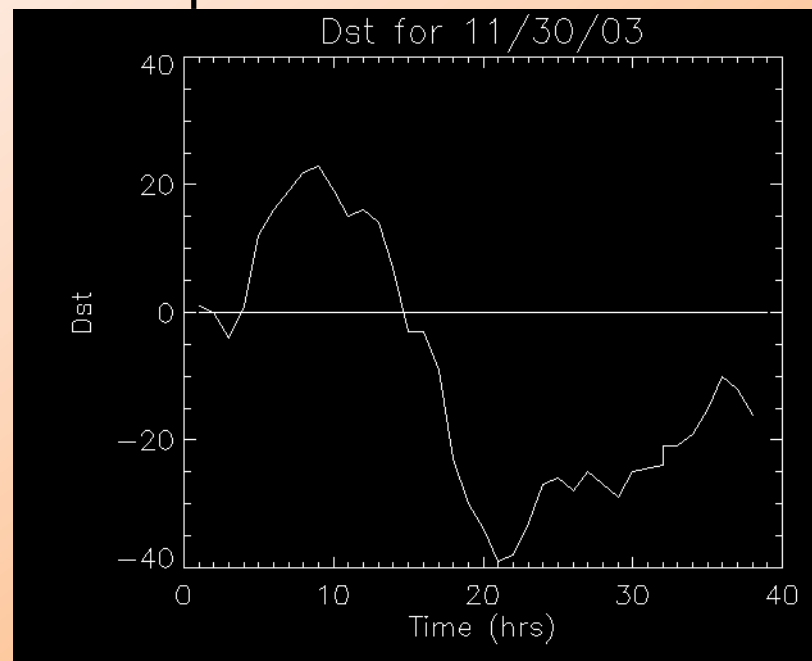


# Methods

- Create visualization techniques to see off-equatorial performance of models
- Compare model outputs of  $|\mathbf{B}|$  to satellite magnetometer measurements
- Bin comparison studies by Kp, Dst, and magnetic latitude

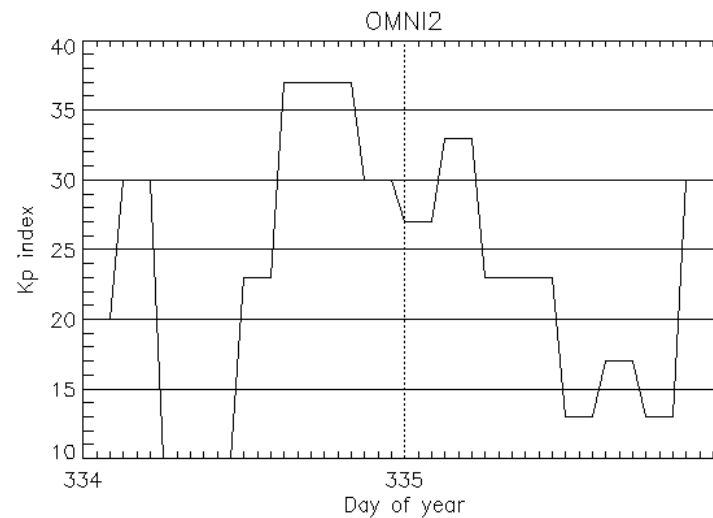
# Some Definitions

- Dst = Geomagnetic Equatorial Index
  - “The Dst index represents the axially symmetric disturbance magnetic field at the dipole equator on the Earth's surface”
  - Define storm sub-phases

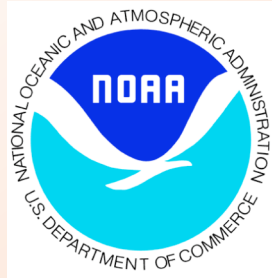


# Some Definitions

- Kp = Geomagnetic activity index
  - ... is a code that is related to the maximum fluctuations of horizontal components observed on a magnetometer relative to a quiet day, during a three-hour interval.
  - $0 \leq Kp \leq 9$



# Why Does NOAA Care ?



- Ultimately understanding how these models perform differently will help forecasting models.
- Scientific research is still performed with “outdated” models.
- Poor off equatorial performance of current models could help to spur the development of new ones.

# Current Knowledge

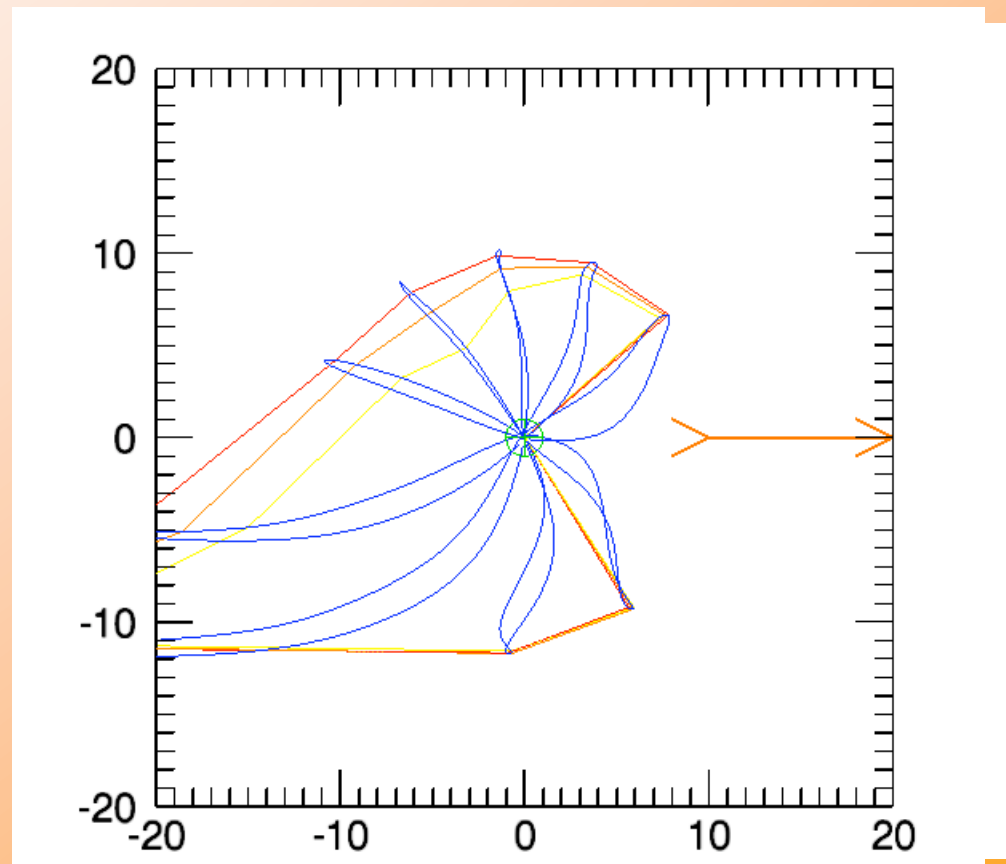
- Equatorial performance on the noonside and midnightside is often poor ( $PE < .5$ ) (anomalous  $B_z$ ) [M<sup>c</sup>Collough *et al* 2008].
- Tsyganenko '96 is popular but is significantly overstretched on the equatorial plane.
- Newer models are more complicated to implement.
- Models show decreased **dawn** and dusk performance at equator [Huang *et al* 2008].

# Magnetic Field Models

- Olson & Pftizer “Dynamic” [1988]
  - Limited input range
  - Only basic physics

View: →

Equatorial high pass filter from  
showing North Pole



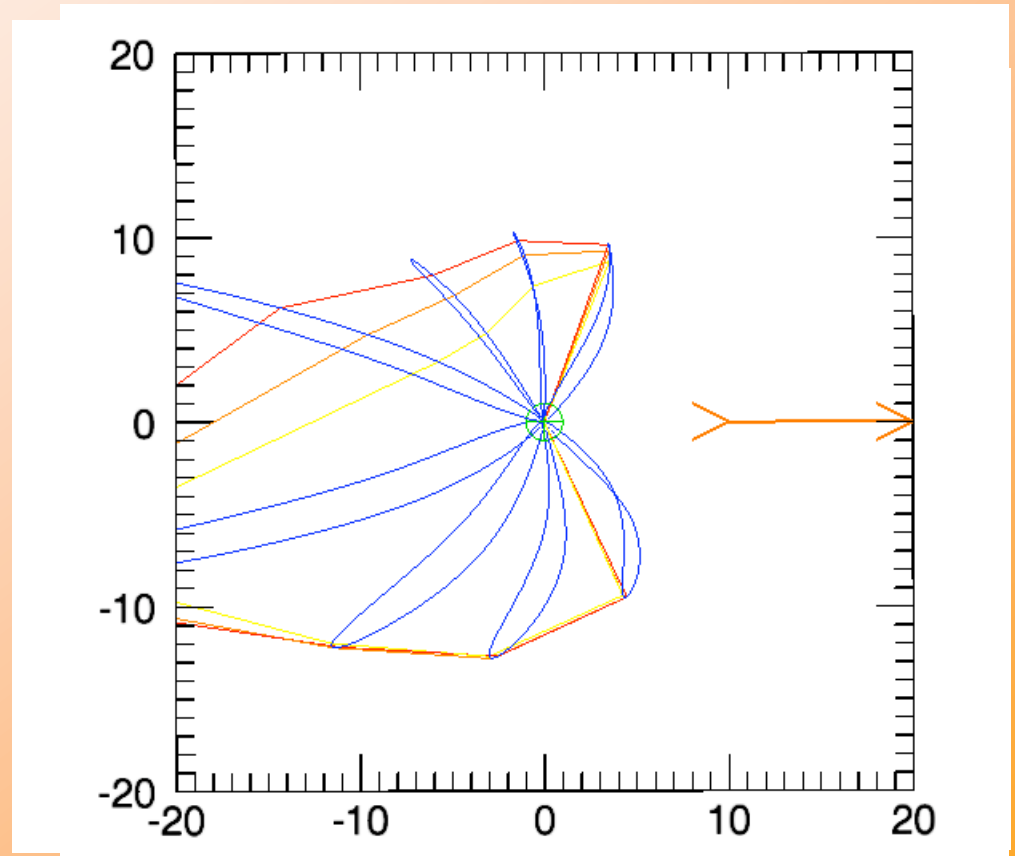


# Magnetic Field Models

- Tsyganenko '96
  - Still commonly used
    - Easy to implement
  - Equatorial field line over-stretching

View: →

Equatorial high-latitude from  
above the North Pole

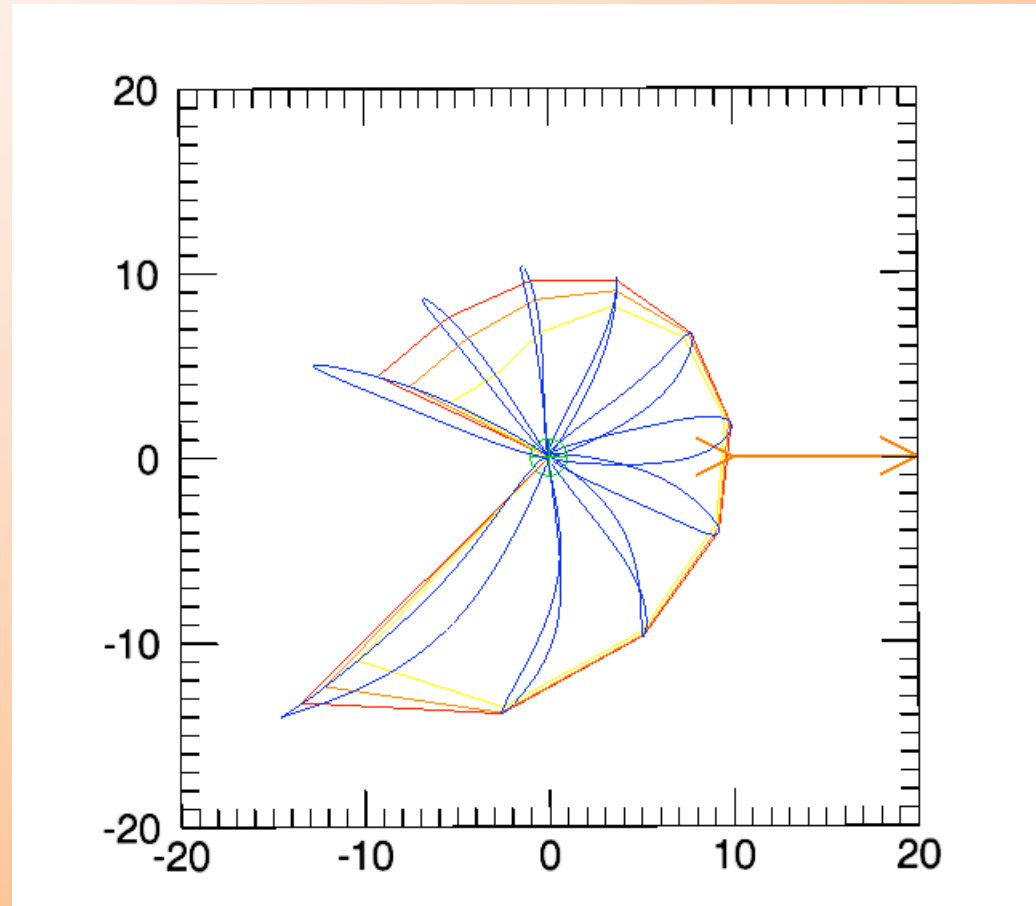


# Magnetic Field Models

- Tsyganenko  
'01/"Storm"  
 – Sibling models  
 – "Storm" has no input constraints  
 – First to allow for time dependence

View: →

Equatorial high-latitude from  
above the North Pole

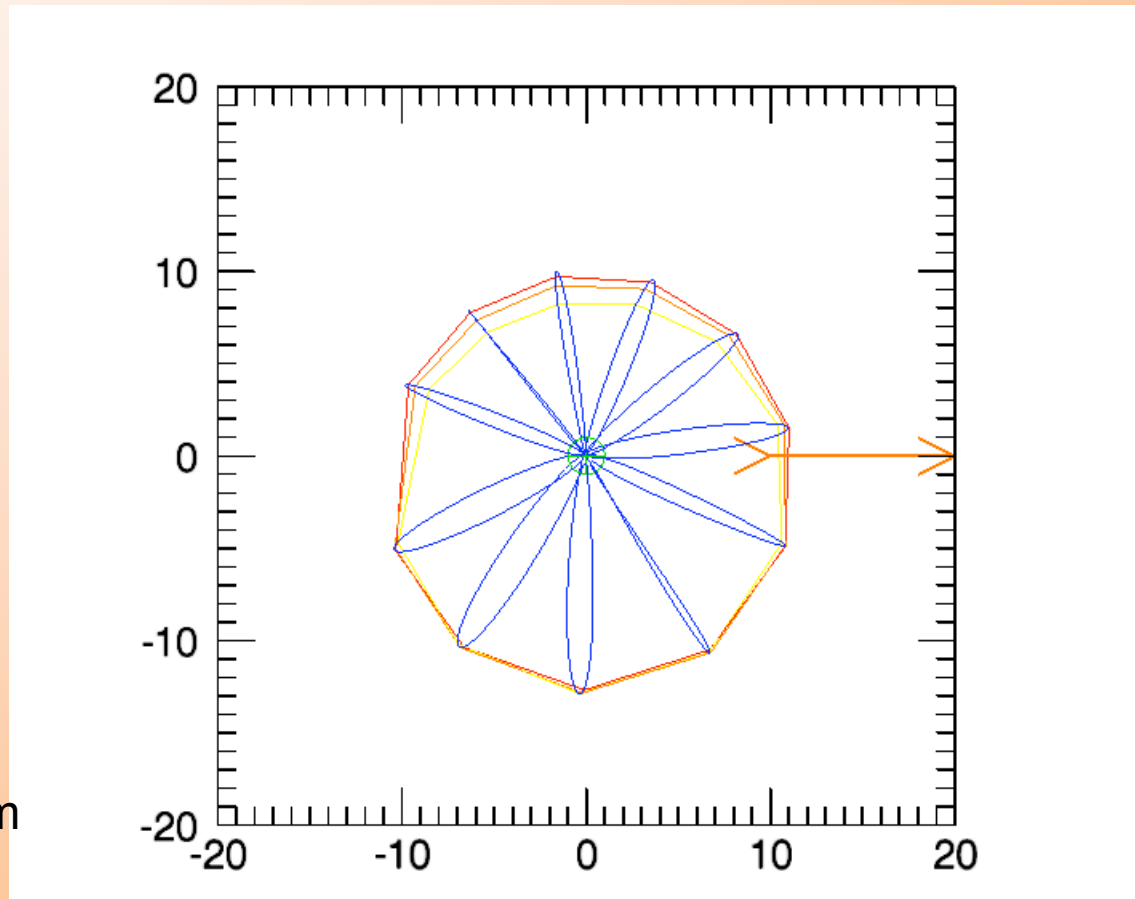


# Magnetic Field Models

- Tsyganenko  
'04

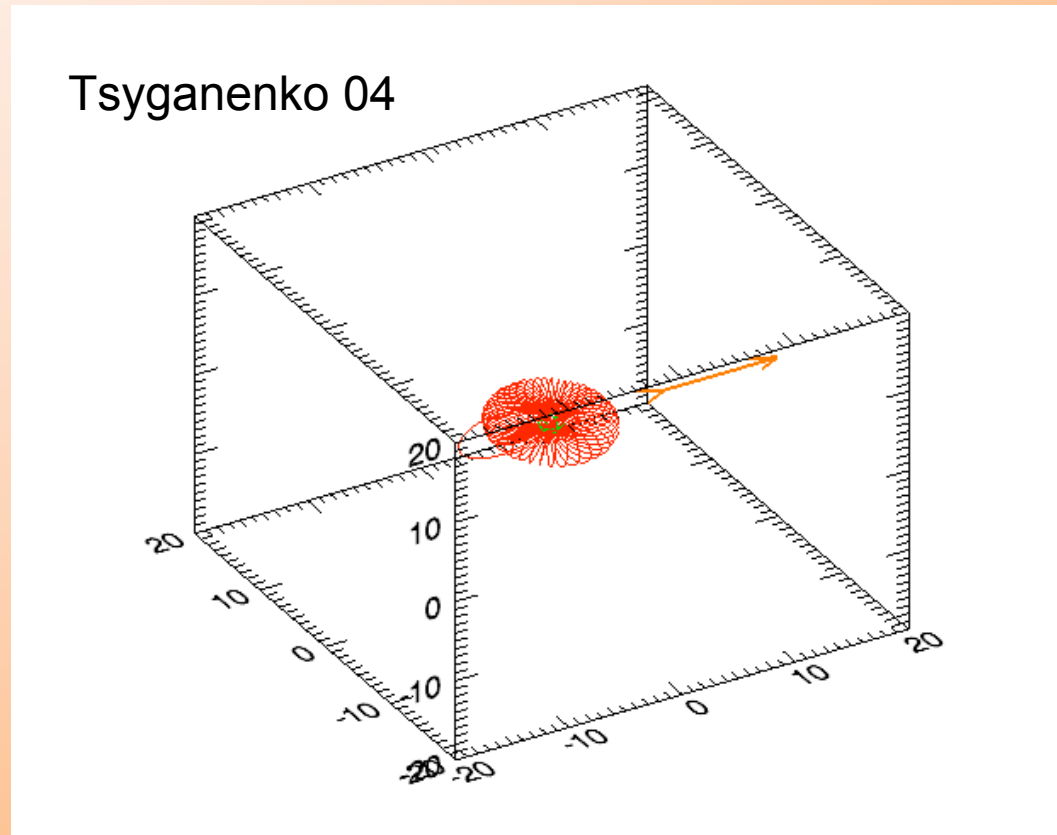
- Newest model available
- Increased time dependence
- Recently touted as providing the best results at the Equator

View:  $\rightarrow$   
 Equatorial plane from  
 North Pole



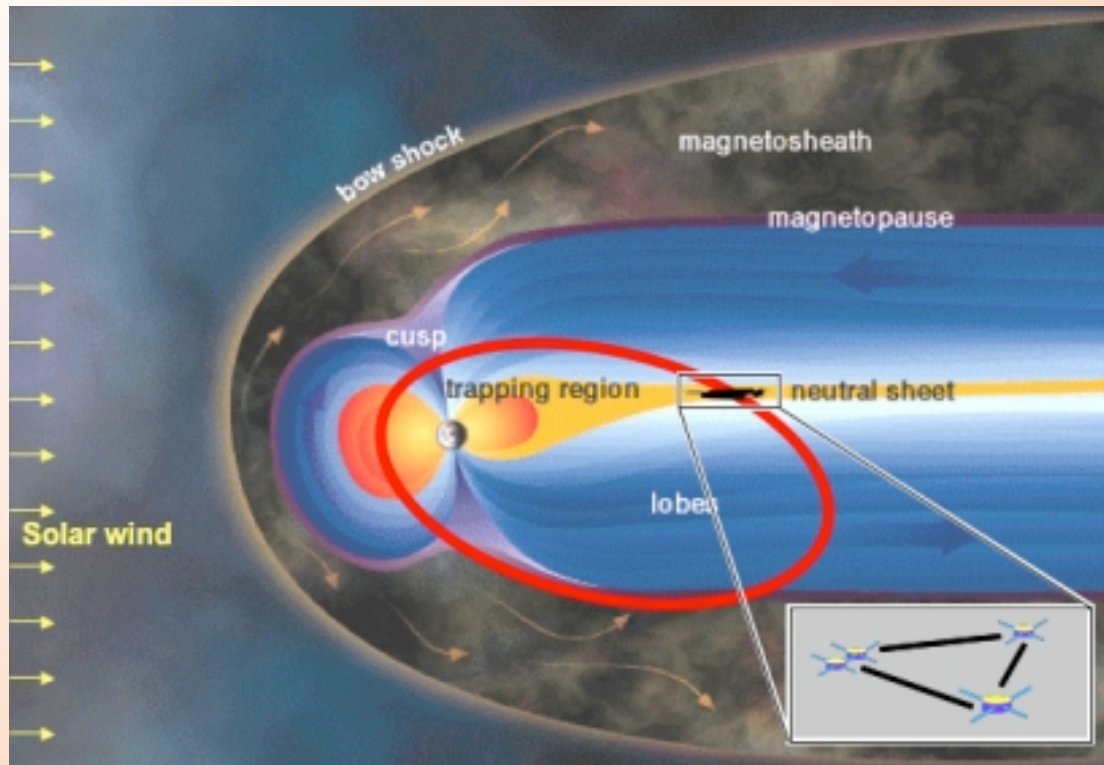
# Drift Shells

- Shapes are similar between models
- Magnitudes are variable
- Results confirm equatorial findings



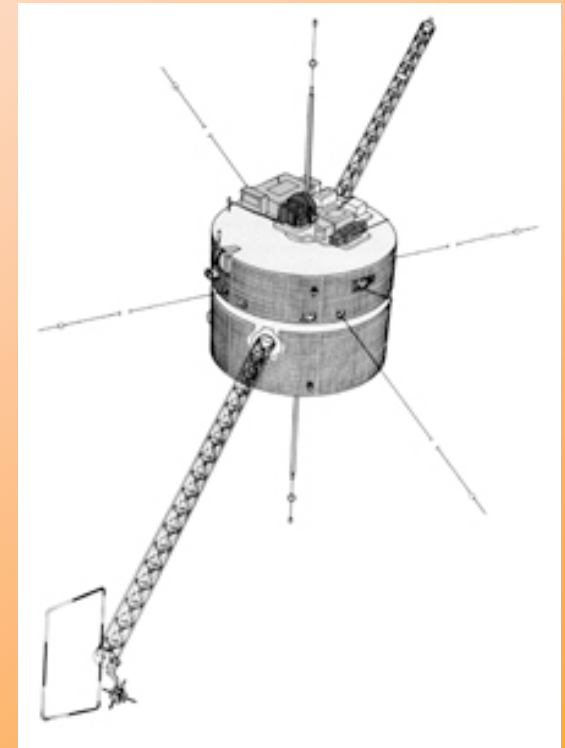
# Satellite Verification of model output $|\mathbf{B}|$ Field

Cluster



<http://clusterlaunch.esa.int/science-e/www/object/index.cfm?fobjectid=41122>

Polar



<http://pwg.gsfc.nasa.gov/polar/>

# Prediction Efficiency

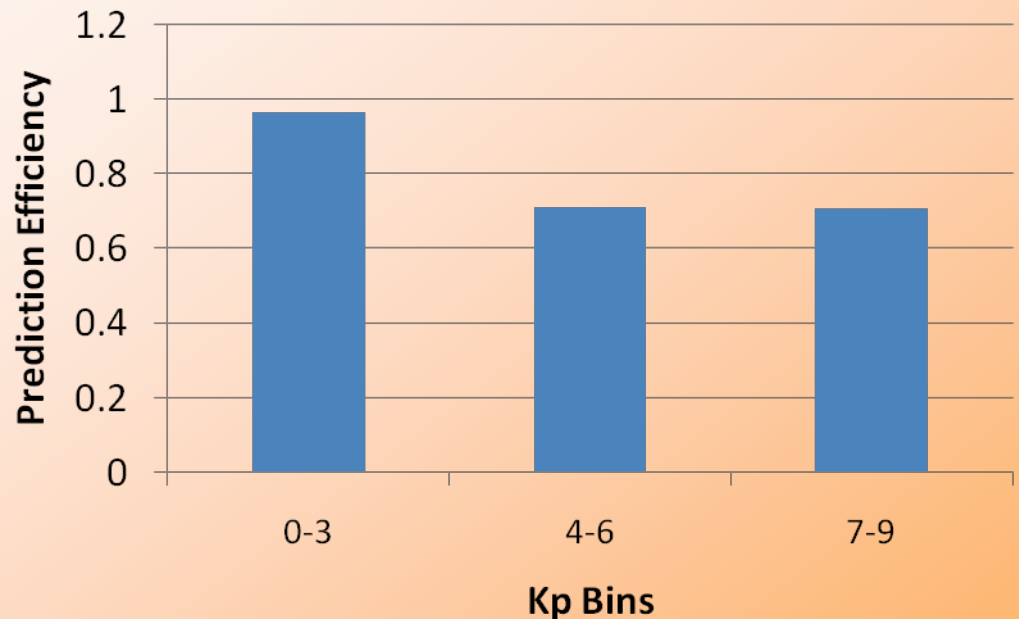
$$PE = 1 - \frac{e_{rms}^2}{\sigma_x^2}$$

Measures how much variation in the data can be explained by the model.

$$e_{rms} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{x}_i - x_i)^2}$$

# Kp Bins

- Divided into...
  - Low (  $0 < k_p < 3$  )
  - Medium (  $4 < k_p < 6$  )
  - High (  $7 < K_p < 9$  )

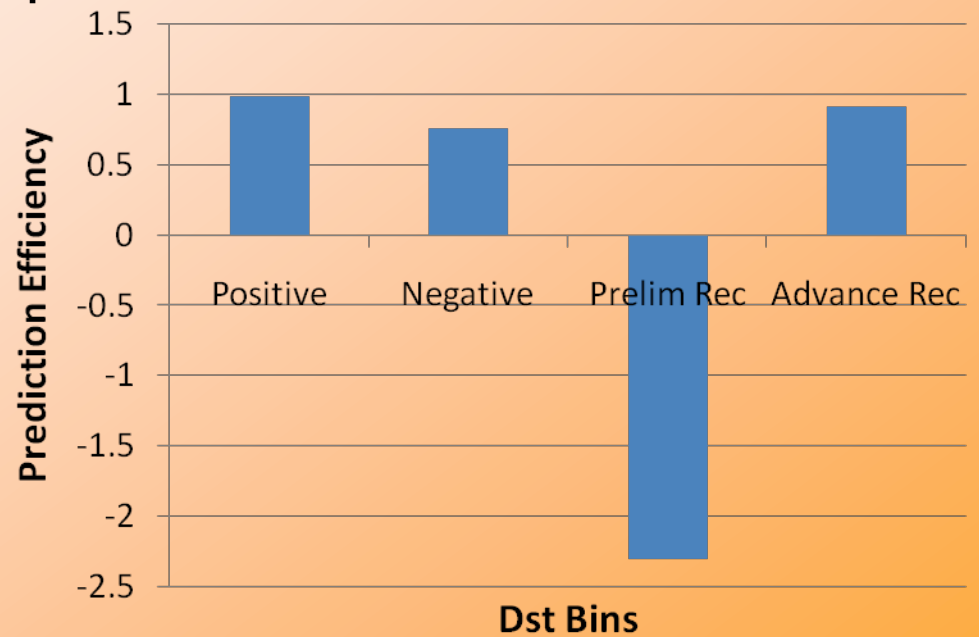


- Lowest bin shows highest prediction efficiency.
- Overall: Tsyganenko '04 has highest PE.
- High Kp: Tsyganenko '01/"Storm" has best PE.



# Dst Bins (Storm Phases)

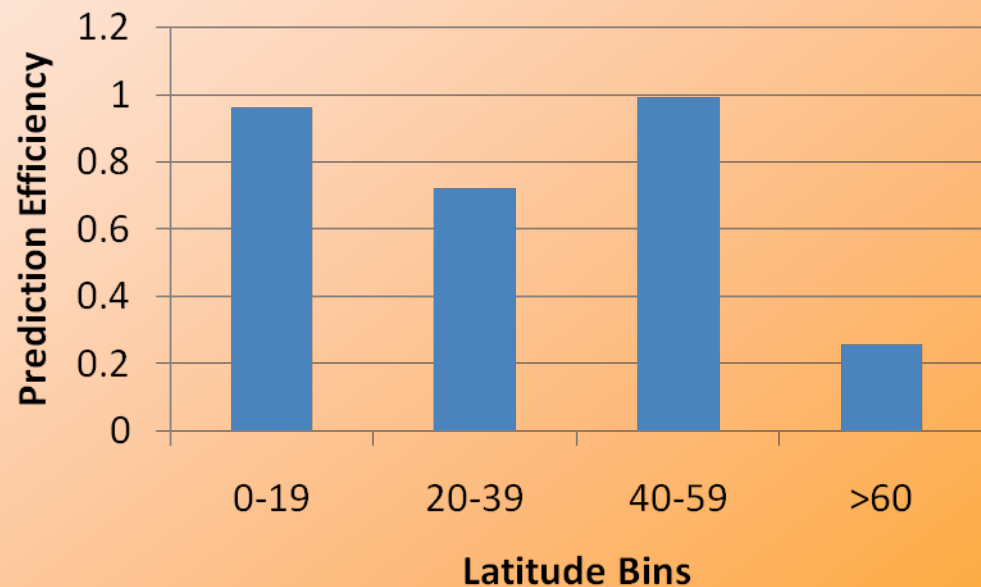
- Divided into: Positive, Negative, Preliminary Recovery, and Advanced Recovery phases.
- Best during Positive and Advanced Recovery
- Overall poor early recovery phase results
- Tsyganenko '04 has best prelim recovery PE probably due to time dependence.





# Magnetic Latitude

- Divided into:  $0^{\circ}$ - $19^{\circ}$ ,  $20^{\circ}$ - $39^{\circ}$ ,  $40^{\circ}$ - $59^{\circ}$ ,  $>60^{\circ}$ .
- $0^{\circ}$ - $19^{\circ}$  and  $40^{\circ}$ - $59^{\circ}$  latitude bins show best performance.
- $>60^{\circ}$  bin shows lowest predictive power.



# Magnetic Latitude Con't

- All three Tsyganenko model perform decently in lowest latitudes. Olson & Pftizer is weakest.
- As latitude increases...
  - Newer models retain robust performance.
  - Older models drop off in performance.
- At highest latitudes, Tsyganenko '01 is best.

# Conclusions

## Overall

- Models perform best in low geomag activity.
- Storm time model performance is best during positive and advanced recovery phases of storms.
- Many of the problems shown in equatorial studies are manifest at higher L values.
- Drift shells are very similar among models.

# Conclusions Con't

## Models

- Overall, Tsyganenko '04 shows best performance statistics.
- During extremely high Kp and at high geomag latitudes, Tsyganenko '01 provides best performance.
- Tsyganenko '96 and Olson & Pfitzer “dynamic” show worst performance.

# Future Work (for the fall)

- Continue to expand the number of data points for better statistics
- Submit for Fall AGU conference
- Write it up and send it off to *Space Weather*

# Wall of Shame

